

## [Help](#)

```
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2010+2) //The "#els
#else

#include <stdio.h>
#include <stdlib.h>
#include <
href../../../../common/math/cdo/cdo_math_h_src.pdfmath.h>
#include "pnl/pnl_vector.h"
#include "pnl/pnl_mathtools.h" // To use the function "pnl_iround"
#include "
href../../../../common/math/InterestRateModelTree/TreeHW1dGeneralized/TreeHW1dGe

// Return the volatility of the short rate
double Current_VolatilityHW1dG(ModelHW1dG *HW1dG, double t)
{
    int i, N;

    i = 0;
    N = (HW1dG->TimeGrid)->size;

    if (HW1dG->TimeGrid == NULL)
    {
        printf("FATALE ERREUR, PAS DE GRILLE DE TEMPS !");
    }

    else
    {
        while (GET(HW1dG->TimeGrid, i) < t && i < N - 1)
        {
            i++;
        }
    }

    return GET(HW1dG->ShortRateVolGrid, i);
}

// Construction of the time grid
int SetTimeGridHW1dG(TreeHW1dG *Meth, int n, double date, double T)
{
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int i;
double delta_time;
int i_date;

Meth->Ngrid = n;
Meth->Tf = T;

Meth->t = pnl_vect_create(n + 2);

delta_time = T / n;

for (i = 0; i <= n + 1; i++)
{
    LET(Meth->t, i) = i * delta_time;
}

i_date = (int) floor(date / delta_time);

if ((i_date > 0) && ((GET(Meth->t, i_date + 1) - date) > delta_time * INC))
{
    LET(Meth->t, i_date) = date;
}

return i_date;
}

int SetTimeGrid_TenorHWldG(TreeHWldG *Meth, int NtY, double T0, double S0, double
{
    int i;
    double delta_time, delta_time1;
    int n, m;

    delta_time = periodicity / NtY;

    n = (int)((S0 - T0) / periodicity + 0.1);
    m = (int) floor(T0 / delta_time);

    delta_time1 = T0 / m;

    Meth->Tf = S0;
    Meth->Ngrid = m + n * NtY;

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Meth->t = pnl_vect_create(Meth->Ngrid + 2);

for (i = 0; i <= m; i++)
{
    LET(Meth->t, i) = i * delta_time1; // Discretization of [0, T0]
}

for (i = m + 1; i <= m + n * NtY + 1; i++)
{
    LET(Meth->t, i) = T0 + (i - m) * delta_time; // Discretization of ]T0, S0]
}

return i;
}

void SetTreeHW1dG(TreeHW1dG *Meth, ModelHW1dG *ModelParam, ZCMarketData *ZCMarketData)
{
    double mean_reversion ;
    double sigma ;

    double Pdown, Pmiddle, Pup;
    double Q2Value, sum_alpha;

    double delta_x1, delta_x2;
    double delta_t1, delta_t2;

    double current_rate;
    double beta_x;
    int jminprev, jmaxprev;
    int jmin, jmax;
    int i, j, h;

    PnlVect *Q1; // Quantity used to calibrate the tree to the initial yield curve
    PnlVect *Q2; // Quantity used to calibrate the tree to the initial yield curve

    mean_reversion = (ModelParam->MeanReversion);

    Meth->Jminimum = pnl_vect_int_create(Meth->Ngrid + 1);
    Meth->Jmaximum = pnl_vect_int_create(Meth->Ngrid + 1);

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pnl_vect_int_set(Meth->Jminimum, 0, 0);
pnl_vect_int_set(Meth->Jmaximum, 0, 0);

pnl_vect_int_set(Meth->Jminimum, 1, -1);
pnl_vect_int_set(Meth->Jmaximum, 1, 1);

// Calcul de alpha(0) et alpha(1)
Meth->alpha = pnl_vect_create(Meth->Ngrid + 1);
Q1 = pnl_vect_create(3);
Q2 = pnl_vect_create(1);

delta_t1 = GET(Meth->t, 1) - GET(Meth->t, 0); // = t[1] - t[0]
delta_t2 = GET(Meth->t, 2) - GET(Meth->t, 1); // = t[2] - t[1]

LET(Meth->alpha, 0) = -log(BondPrice(GET(Meth->t, 1), ZCMarket)) / delta_t1; /

Pup = 1.0 / 6.0;
Pmiddle = 2.0 / 3.0;
Pdown = 1 - Pmiddle - Pup;

LET(Q1, 0) = Pdown * exp(- GET(Meth->alpha, 0) * delta_t1); // Q(1,-1)
LET(Q1, 1) = Pmiddle * exp(- GET(Meth->alpha, 0) * delta_t1); // Q(1,0)
LET(Q1, 2) = Pup * exp(- GET(Meth->alpha, 0) * delta_t1); // Q(1,-2)

sigma = Current_VolatilityHW1dG(ModelParam, GET(Meth->t, 1)); // sigma(t1)

delta_x1 = SpaceStepHW1dG(delta_t1, sigma); //SpaceStepHW1dG(delta_t1, a, sigma

sum_alpha = GET(Q1, 0) * exp(delta_x1 * delta_t2) + GET(Q1, 1) + GET(Q1, 2) *

LET(Meth->alpha, 1) = log(sum_alpha / BondPrice(GET(Meth->t, 2), ZCMarket)) /

jmin = -1;
jmax = 1;

for (i = 1; i < Meth->Ngrid ; i++)
{
    delta_t1 = GET(Meth->t, i) - GET(Meth->t, i - 1); // = t[i] - t[i-1]
    delta_t2 = GET(Meth->t, i + 1) - GET(Meth->t, i); // = t[i+1] - t[i]

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sigma = Current_VolatilityHW1dG(ModelParam, GET(Meth->t, i)); // sigma(ti)
delta_x1 = SpaceStepHW1dG(delta_t1, sigma); // delta_x[i]
sigma = Current_VolatilityHW1dG(ModelParam, GET(Meth->t, i + 1)); // sigma
delta_x2 = SpaceStepHW1dG(delta_t2, sigma); // delta_x[i+1]

beta_x = delta_x1 / delta_x2;

jminprev = jmin; // jminprev := jmin[i]
jmaxprev = jmax; // jmaxprev := jmax[i]

jmin = pnl_iround(jminprev * beta_x * exp(-delta_t2 * mean_reversion)) - 1
jmax = pnl_iround(jmaxprev * beta_x * exp(-delta_t2 * mean_reversion)) + 1

pnl_vect_int_set(Meth->Jminimum, i + 1, jmin);
pnl_vect_int_set(Meth->Jmaximum, i + 1, jmax);

pnl_vect_resize(Q2, jmax - jmin + 1); // Q1 :=Q(i,.) et Q2 :=Q(i+1,.)

pnl_vect_set_double(Q2, 0);

for (h = jminprev ; h <= jmaxprev ; h++)
{
    current_rate = GET(Meth->alpha, i) + h * delta_x1;

    j = pnl_iround(h * beta_x * exp(-delta_t2 * mean_reversion)); //j index

    // Probability to go from (i,h) to (i+1,j+1) with an UP movement
    Pup = ProbaUpHW1dG(h, j, delta_t2, beta_x, mean_reversion);
    // Probability to go from (i,h) to (i+1,j) with a Middle movement
    Pmiddle = ProbaMiddleHW1dG(h, j, delta_t2, beta_x, mean_reversion);
    // Probability to go from (i,h) to (i+1,j-1) with a Down movement
    Pdown = 1 - Pup - Pmiddle;

    Q2Value = GET(Q2, j + 1 - jmin) + GET(Q1, h - jminprev) * Pup * exp(-c
    LET(Q2, j + 1 - jmin) = Q2Value;

    Q2Value = GET(Q2, j - jmin) + GET(Q1, h - jminprev) * Pmiddle * exp(-c
    LET(Q2, j - jmin) = Q2Value;

    Q2Value = GET(Q2, j - 1 - jmin) + GET(Q1, h - jminprev) * Pdown * exp(-c
    LET(Q2, j - 1 - jmin) = Q2Value;

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    } //END loop over h

    delta_t2 = GET(Meth->t, i + 2) - GET(Meth->t, i + 1);
    sum_alpha = 0;
    for (j = jmin ; j <= jmax ; j++)
    {
        sum_alpha += GET(Q2, j - jmin) * exp(-j * delta_x2 * delta_t2);
    }

    LET(Meth->alpha, i + 1) = log(sum_alpha / BondPrice(GET(Meth->t, i + 2), Z

    pnl_vect_clone(Q1, Q2);

} // End Loop on i

pnl_vect_free(&Q1);
pnl_vect_free(&Q2);

} // FIN de la fonction SetTreeHW1dG

// Backward computation of the price of a product from time Meth->t[index_last]
// The initial value of the product (at time Meth->t[index_last]) is the vector
void BackwardIterationHW1dG(TreeHW1dG *Meth, ModelHW1dG *ModelParam, PnlVect *Op
{
    double mean_reversion;
    double sigma;

    int jmin; // jmin[i+1], jmax[i+1]
    int jminprev, jmaxprev; // jmin[i], jmax [i]
    int i, j, k;
    double Pup, Pdown, Pmiddle;
    double delta_x1, delta_x2, beta_x;
    double delta_t1, delta_t2;
    double current_rate;

    ///*****Parameters of the process r *****///
    mean_reversion = (ModelParam->MeanReversion);

    jminprev = pnl_vect_int_get(Meth->Jminimum, index_last); // jmin(index_last)

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jmaxprev = pnl_vect_int_get(Meth->Jmaximum, index_last); // jmax(index_last)

for (i = index_last - 1; i >= index_first; i--)
{
    jmin = jminprev; // jmin := jmin(i+1)

    jminprev = pnl_vect_int_get(Meth->Jminimum, i); // jmin(i)
    jmaxprev = pnl_vect_int_get(Meth->Jmaximum, i); // jmax(i)

    pnl_vect_resize(OptionPriceVect1, jmaxprev - jminprev + 1); // OptionPrice

    delta_t1 = GET(Meth->t, i) - GET(Meth->t, i - 1); // Time step between t[i]
    delta_t2 = GET(Meth->t, i + 1) - GET(Meth->t, i); // Time step between t[i]

    sigma = Current_VolatilityHW1dG(ModelParam, GET(Meth->t, i)); // sigma(ti)
    delta_x1 = SpaceStepHW1dG(delta_t1, sigma); // SpaceStepHW1dG(delta_t1, a, s)

    sigma = Current_VolatilityHW1dG(ModelParam, GET(Meth->t, i + 1)); // sigma
    delta_x2 = SpaceStepHW1dG(delta_t2, sigma); // SpaceStepHW1dG(delta_t2, a, s)

    beta_x = delta_x1 / delta_x2;

    // Loop over the node at the time i
    for (j = jminprev ; j <= jmaxprev ; j++)
    {
        k = pnl_iround(j * beta_x * exp(-delta_t2 * mean_reversion)); // h inde

        // Probability to go from (i,j) to (i+1,k+1) with an UP movement
        Pup = ProbaUpHW1dG(j, k, delta_t2, beta_x, mean_reversion);
        // Probability to go from (i,j) to (i+1,k) with a Middle movement
        Pmiddle = ProbaMiddleHW1dG(j, k, delta_t2, beta_x, mean_reversion);
        // Probability to go from (i,j) to (i+1,k-1) with a Down movement
        Pdown = 1 - Pup - Pmiddle;

        current_rate = j * delta_x1 + GET(Meth->alpha, i); // r(i,j)

        LET(OptionPriceVect1, j - jminprev) = exp(-current_rate * delta_t2) *
    }

    pnl_vect_clone(OptionPriceVect2, OptionPriceVect1); // Copy OptionPriceVec

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    } // END of the loop on i (time)
}

// To locate the date s inf the tree. t[IndexTime(s)-1]< s <= t[IndexTime(s)]
int IndexTimeHW1dG(TreeHW1dG *Meth, double s)
{
    int i = 0;

    if (Meth->t == NULL)
    {
        printf("FATALE ERREUR, PAS DE GRILLE DE TEMPS !");
    }
    else
    {
        while (GET(Meth->t, i) < s && i <= Meth->Ngrid)
        {
            i++;
        }
    }
    return i;
}

// Return Delta_x(i)
double SpaceStepHW1dG(double delta_t, double sigma)
{
    return sigma * sqrt(3 * delta_t);
}

// Probability to go from (i, j) to (i, k+1) with an Up movement
double ProbaUpHW1dG(int j, int k, double delta_t2, double beta_x, double mean_re
{
    double alpha;

    alpha = j * beta_x * exp(-mean_reversion * delta_t2) - k;

    return 1. / 6. + alpha * (alpha + 1) / 2;
}

// Probability to go from (i, j) to (i, k) with a Middle movement
double ProbaMiddleHW1dG(int j, int k, double delta_t2, double beta_x, double mea
{

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double alpha;

alpha = j * beta_x * exp(-mean_reversion * delta_t2) - k;

return 2. / 3. - alpha * alpha;
}

// Probability to go from (i, j) to (i, k-1) with a Down movement
double ProbaDownHW1dG(int j, int k, double delta_t2, double beta_x, double mean_
{
    double alpha;

    alpha = j * beta_x * exp(-mean_reversion * delta_t2) - k;

    return 1. / 6. + alpha * (alpha - 1) / 2;
}

int DeleteTimegridHW1dG(struct TreeHW1dG *Meth)
{
    pnl_vect_free(&(Meth->t));
    return 1;
}

int DeleteTreeHW1dG(struct TreeHW1dG *Meth)
{
    pnl_vect_int_free(&(Meth->Jmaximum));
    pnl_vect_int_free(&(Meth->Jminimum));

    pnl_vect_free(&(Meth->alpha));

    DeleteTimegridHW1dG(Meth);
    return 1;
}

int DeletModelHW1dG(struct ModelHW1dG *HW1dG)
{
    pnl_vect_free(&(HW1dG->TimeGrid));
    pnl_vect_free(&(HW1dG->ShortRateVolGrid));

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    return 1;
}

#endif //PremiaCurrentVersion
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