

## Help

```
#include <stdlib.h>
#include <stdio.h>
#include <string.h>
#include <
href../../../../common/math/cdo/cdo_math_h_src.pdfmath.h>
#include <assert.h>

#include "pnl/pnl_fft.h"
#include "pnl/pnl_specfun.h"
#include "pnl/pnl_finance.h"
#include "pnl/pnl_band_matrix.h"
#include "pnl/pnl_complex.h"
#include "pnl/pnl_matrix.h"
#include "pnl/pnl_mathtools.h"

#include "
href../../../../common/math/equity_pricer/pde_tools_h_src.pdfpde_tools.h"
#include "
href../../../../common/math/equity_pricer/levy_process_h_src.pdflevy_process.h"

#define IMPLICIT_VOL 0.0000
#define EPSILON_CALIBRATION 1e-2

#define GETPROCESSPARAMETER(v,i){          \
    if (i>=v->nb_parameters || i<0){        \
        perror("index out of range"); abort();}\
    else{return ((double *)v)[i];}}

#define SETPROCESSPARAMETER(v,i,a){        \
    if (i>=v->nb_parameters || i<0){        \
        perror("index out of range"); abort();}\
    else{((double *)v)[i]=a;}}

#define GETLEVYPARAMETER(v,i){              \
    if (i>=v->nb_parameters || i<0){        \
        perror("index out of range"); abort();}\
    else{return ((double *)v->process)[i];}}

#define SETLEVYPARAMETER(v,i,a){            \
```

```

if (i>=v->nb_parameters || i<0){          \
    perror("index out of range"); abort();} \
else{((double *)v->process)[i]=a;}}

/**
 * ln ( Gamma_ln (z+1)/z )
 * where Gamma_ln(z)=int_R^+ log(t) t^{z-1} exp(-t) dt,
 * the logarithm of the Gamma_log function
 * @param z  a complex number
 * @return ln (Gamma (z))
 */
dcomplex Clgamma_log(dcomplex z)
{
    dcomplex x, y, tmp, ser, sersq;
    static double cof[6] = {76.18009172947146, -86.50532032941677,
                           24.01409824083091, -1.231739572450155,
                           0.1208650973866179e-2, -0.5395239384953e-5
                           };

    double gamma = 5;
    int j;

    if (z.r < 0)
        PNL_ERROR("Error in Clgamma_log !", "Real part are not positive, CGMY.c ");
    y = x = z;
    tmp = Cadd(x, Complex(gamma + 0.5, 0));
    sersq = CZERO;
    ser = Complex(1.000000000190015, 0.0);

    for (j = 0; j <= 5; j++)
    {
        y = Cadd(y, CUNO);
        ser = Cadd(ser, Cdiv(Complex(cof[j], 0), y));
        sersq = Cadd(sersq, Cdiv(Complex(cof[j], 0), Cmul(y, y)));
    }

    ser = Cmul(Csub(Clog(tmp), Cdiv(Complex(gamma, 0), tmp)), ser);
    ser = Csub(ser, sersq);
    ser = RCMul(sqrt(M_2PI), ser);
    tmp = Csub(Cmul(Cadd(x, Complex(0.5, 0)), Clog(tmp)), tmp);
    return Cadd(Clog(Cdiv(ser, x)), tmp);
}

```

```
}
```

```
dcomplex Ctgamma_log(dcomplex z)
{
    if (z.r < 0)
        return Cdiv(Csub(Ctgamma_log(Complex(z.r + 1, 0)), Ctgamma(z)), z);
    return Csub(Cexp(Clgamma_log(z)), Cdiv(Cexp(Clgamma(z)), z));
}
```

```
double tbeta(double a, double b)
{
    return exp(pnl_lgamma(a) + pnl_lgamma(b) - pnl_lgamma(a + b));
}
```

```
dcomplex Ctbeta(dcomplex a, dcomplex b)
{
    return Cexp(Csub(Cadd(Clgamma(a), Clgamma(b)), Clgamma(Cadd(a, b))));
}
```

```
/*
dcomplex BS_characteristic_exponent(dcomplex u, BS_process * mod)
{
    // Test with BS process
    double vol_square = mod->vol;
    double r = mod->r;
    //>> Case 1 code infinitesimal generator of backward k=i-j
    return Complex(vol_square*u.r*u.r, -(r-vol_square)*u.r);
    //>> Case 2 code infinitesimal generator of diffusion k=j-i and use
    //>> bar(psi)(-u) = psi(u)
    //return Complex(vol_square*u.r*u.r, (r-vol_square)*u.r);
}
*/
```

```
static dcomplex M_minus_i_u_pow_Y_minus_M_pow_Y(dcomplex u, double Y, double M,
{

    double r = pow(M + u.i, 2) + u.r * u.r;
    // Problem with too small value of M, ?
```

```

double theta = atan(-u.r / (M + u.i)) * Y;
// Test of stabilized formula :
// double x=-u.r/(M+u.i);
// double theta = (fabs(x)<1)?atan(x):((x>0)?1:-1)*M_PI_2-atan(1./x);
// theta *=Y;
r = pow(r, Y / 2);
return Complex(r * cos(theta) - MpowY, r * sin(theta));
}

static dcomplex characteristic_exponent_cgmy(dcomplex u, double G, double M, dou
{
    return Cadd(M_minus_i_u_pow_Y_minus_M_pow_Y(u, Y, M, MpowY),
                M_minus_i_u_pow_Y_minus_M_pow_Y(CRmul(u, -1), Y, G, GpowY));
}

// ----- BS -----

dcomplex BS_process_characteristic_exponent_without_cast(dcomplex u, BS_process
{
    dcomplex psi = C_op_amib(RCmul(0.5 * mod->sigma, Cmul(u, u)), RCmul(mod->rate
    return CRadd(psi, mod->rate);
}

dcomplex BS_process_characteristic_exponent(dcomplex u, void *mod)
{
    return BS_process_characteristic_exponent_without_cast(u, (BS_process *) mod);
}

BS_process *BS_process_create(double sigma, double rate, double *jump_drift)
{
    BS_process *process = malloc(sizeof(BS_process));
    process->sigma = sigma;
    process->rate = rate;
    process->nb_parameters = 2;

    //>> Two way to compute drift term due to jump,
    //>> Put on Band matrix

```

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    (*jump_drift) = 0;
    //>> Or Put in FD scheme (comment previous line and uncomment to next line)
    // (*jump_drift)= -process->C_Gamma_minus_Alpha_Minus*process->LambdapowAlphaMinus=0.0;
    //process->LambdapowAlphaMinus=0.0;
    return process;
};

BS_process *BS_process_create_from_vect(const PnlVect *input)
{
    int i;
    BS_process *process = malloc(sizeof(BS_process));
    process->nb_parameters = 2;
    for (i = 0; i < process->nb_parameters; i++)
        SETPROCESSPARAMETER(process, i, GET(input, i));
    return process;
};

void BS_process_update_cast(void *process)
{};

// ----- Merton -----

dcomplex Merton_process_characteristic_exponent_without_cast(dcomplex u, Merton_
{
    dcomplex u_sqr_plus_i_u = Cmul(u, Complex(u.r, u.i + 1));
    dcomplex psi = C_op_amib(RCmul(0.5 * mod->sigma, u_sqr_plus_i_u), RCmul(mod->r
    /*
        dcomplex psi_J=RCmul(-mod->sigmaj_sqr_demi,u_sqr_plus_i_u);
        psi_J=C_op_apib(psi_J,RCmul(mod->lnonepmuj,u));
        psi_J=RCadd(-1,Cexp(psi_J));
    */
    dcomplex psi_J = C_op_apib(RCmul(-mod->sigmaj_sqr_demi, Cmul(u, u)), RCmul(mod
    psi_J = Csub(Cexp(psi_J), CUNO);
    psi = Csub(psi, RCmul(mod->Lambda_J, psi_J));
    psi = C_op_apib(psi, CRmul(u, mod->Drift));
    return CRadd(psi, mod->rate);
}

```

```

dcomplex Merton_process_characteristic_exponent(dcomplex u, void *mod)
{
    return Merton_process_characteristic_exponent_without_cast(u, (Merton_process
}
void Merton_process_update(Merton_process *process)
{
    process->sigmaj_sqr_demi = 0.5 * process->Sigma_J * process->Sigma_J;
    process->lnonepmuj = log(1 + process->mu_J);
    process->Drift = process->Lambda_J * (exp(process->mu_J + process->sigmaj_sqr_
}

Merton_process *Merton_process_create(double sigma, double rate,
                                     double mu_J_, double Sigma_J_, double Lamb

{
    Merton_process *process = malloc(sizeof(Merton_process));
    process->sigma = sigma;
    process->rate = rate;
    process->mu_J = mu_J_;
    process->Sigma_J = Sigma_J_;
    process->Lambda_J = Lambda_J_;
    process->nb_parameters = 5;
    //>> Two way to compute drift term due to jump,
    //>> Put on Band matrix
    (*jump_drift) = 0;
    //>> Or Put in FD scheme (comment previous line and uncomment to next line)
    // (*jump_drift)= -process->C_Gamma_minus_Alpha_Minus*process->Lambdap1powAlp
    //process->Lambdap1powAlphaMinus=0.0;
    return process;
};

Merton_process *Merton_process_create_from_vect(const PnlVect *input)
{
    int i;
    Merton_process *process = malloc(sizeof(Merton_process));
    process->nb_parameters = 5;
    for (i = 0; i < process->nb_parameters; i++)
        SETPROCESSPARAMETER(process, i, GET(input, i));
    Merton_process_update(process);
    return process;
};

```

```

void Merton_process_update_cast(void *process)
{
    Merton_process_update((Merton_process *)process);
}

// ----- CGMY -----

dcomplex CGMY_process_characteristic_exponent_without_cast(dcomplex u, CGMY_proc
{

    //>> To add special cas Y=0 and Y=1 (Gamma not defined )

    //>> Case 1 code infinitesimal generator of backward k=i-j
    dcomplex psi = characteristic_exponent_cgmy(u, mod->G, mod->M, mod->Y, mod->Mp
    psi = C_op_amib(psi, CRmul(u, mod->Mm1powY));
    return RCmul(-mod->C_Gamma_minus_Y, psi);
    //>> Case 2 code infinitesimal generator of diffuison k=j-i and use
    //>> bar(psi)(-u) = psi(u)
    /*
        To do
        dcomplex psi =characteristic_exponent_cgmy(u,mod->G,mod->M,mod->Y,mod->MpowY
        psi=C_op_amib(psi,CRmul(u,mod->Mm1powY));
        return RCmul(-mod->C_Gamma_minus_Y,psi);
    */
}

dcomplex CGMY_process_characteristic_exponent(dcomplex u, void *mod)
{
    return CGMY_process_characteristic_exponent_without_cast(u, (CGMY_process *) m
}

void CGMY_process_update(CGMY_process *process)
{
    process->GpowY = pow(process->G, process->Y);
    process->MpowY = pow(process->M, process->Y);
    process->C_Gamma_minus_Y = process->C * pnl_tgamma(-process->Y);
    process->Gp1powY = pow(process->G + 1, process->Y) - process->GpowY;
}

```

```

    process->Mm1powY = pow(process->M - 1, process->Y) - process->MpowY + process->M;
}

```

```

CGMY_process *CGMY_process_create(double C, double G, double M, double Y, double
{
    CGMY_process *process = malloc(sizeof(CGMY_process));
    process->C = C;
    process->G = G;
    process->M = M;
    process->Y = Y;
    process->nb_parameters = 4;
    CGMY_process_update(process);
    //printf(" Jump drift correction plus %7.4f \ n",-process->C_Gamma_minus_Y*process->Mm1powY);
    //printf(" Jump drift correction %7.4f \ n",-process->C_Gamma_minus_Y*process->Mm1powY);
    //>> Two way to compute drift term due to jump,
    //>> Put on Band matrix
    (*jump_drift) = 0;
    //>> Or Put in FD scheme (comment previous line and uncomment to next line)
    //(*jump_drift)= -process->C_Gamma_minus_Y*process->Mm1powY;
    //process->C_Gamma_minus_Y*process->Mm1powY=0;

    process->levyp = process->M;
    process->levyn = process->G;
    process->levynu = 1.;
    return process;
};

```

```

CGMY_process *CGMY_process_create_from_vect(const PnlVect *input)
{
    int i;
    CGMY_process *process = malloc(sizeof(CGMY_process));
    process->nb_parameters = 4;
    for (i = 0; i < process->nb_parameters; i++)
        SETPROCESSPARAMETER(process, i, GET(input, i));
    CGMY_process_update(process);
    return process;
};

```

```

void CGMY_process_update_cast(void *process)
{

```



```

    CGMY_process_update((CGMY_process *)process);
}

// ----- Temperedstable -----

dcomplex Temperedstable_process_characteristic_exponent_without_cast(dcomplex u,
{
    //>> Case 1 code infinitesimal generator of backward  $k=i-j$ 
    dcomplex psiplus = M_minus_i_u_pow_Y_minus_M_pow_Y(u, mod->AlphaPlus, mod->La
    dcomplex psiminus = M_minus_i_u_pow_Y_minus_M_pow_Y(Complex(-u.r, -u.i), mod->
    psiplus = C_op_amib(psiplus, CRmul(u, mod->Lambdam1powAlphaPlus));
    psiminus = C_op_amib(psiminus, CRmul(u, mod->Lambdap1powAlphaMinus));
    psiplus = Cadd(RCmul(-mod->C_Gamma_minus_Alpha_Plus, psiplus), RCmul(-mod->C_G
    // Now substract implicate diffusion term
    return psiplus;
    //>> Case 2 code infinitesimal generator of diffusion  $k=j-i$  and use
    //>>  $\bar{\psi}(-u) = \psi(u)$ 
    // To do
}

dcomplex Temperedstable_process_characteristic_exponent(dcomplex u, void *mod)
{
    return Temperedstable_process_characteristic_exponent_without_cast(u, (Temper
}

void Temperedstable_process_update(Temperedstable_process *process)
{
    process->LambdapowAlphaPlus = pow(process->LambdaPlus, process->AlphaPlus);
    process->LambdapowAlphaMinus = pow(process->LambdaMinus, process->AlphaMinus);
    process->Lambdam1powAlphaPlus = pow(process->LambdaPlus - 1.0, process->AlphaP
    process->Lambdap1powAlphaMinus = pow(process->LambdaMinus + 1.0, process->Alph
    process->C_Gamma_minus_Alpha_Plus = process->CPlus * pnl_tgamma(-process->Alph
    process->C_Gamma_minus_Alpha_Minus = process->CMinus * pnl_tgamma(-process->Al
}

Temperedstable_process *Temperedstable_process_create(double AlphaPlus, double A
    double LambdaMinus, double CPlus, double CMinus, double *jump_drift)
{
    Temperedstable_process *process = malloc(sizeof(Temperedstable_process));
    process->AlphaPlus = AlphaPlus;
    process->AlphaMinus = AlphaMinus;

```

```

process->LambdaPlus = LambdaPlus;
process->LambdaMinus = LambdaMinus;
process->CPlus = CPlus;
process->CMinus = CMinus;
process->nb_parameters = 6;
Temperedstable_process_update(process);
//printf(" Jump drift correction Plus %7.4f \ n", -process->C_Gamma_minus_Alpha
//printf(" Jump drift correction Minus %7.4f \ n",-process->C_Gamma_minus_Alpha
//>> Two way to compute drift term due to jump,
//>> Put on Band matrix
(*jump_drift) = 0.; //-(process->C_Gamma_minus_Alpha_Plus*process->Lambdam1pow
//process->Lambdam1powAlphaPlus=0;
//process->Lambdap1powAlphaMinus=0;
//>> Or Put in FD scheme (comment previous line and uncomment to next line)
// (*jump_drift)= -process->C_Gamma_minus_Alpha_Minus*process->Lambdap1powAlp
//process->Lambdap1powAlphaMinus=0.0;

return process;
};

Temperedstable_process *Temperedstable_process_create_from_vect(const PnlVect *i
{
    int i;
    Temperedstable_process *process = malloc(sizeof(Temperedstable_process));
    process->nb_parameters = 6;
    for (i = 0; i < process->nb_parameters; i++)
        SETPROCESSPARAMETER(process, i, GET(input, i));
    Temperedstable_process_update(process);
    return process;
};

void Temperedstable_process_update_cast(void *process)
{
    Temperedstable_process_update((Temperedstable_process *)process);
}

// ----- NIG -----

dcomplex NIG_process_characteristic_exponent_without_cast(dcomplex u, NIG_proces
{

```

```

dcomplex psi = C_op_apib(Complex(mod->Beta, 0), u);
psi = Cmul(psi, psi);
psi = CRsub(Csqrt(RCsub(mod->Alpha_sqr, psi)), mod->Sqrt_Alpha2_minus_Beta2);
psi = RCmul(mod->Delta, C_op_amib(psi, RCmul(mod->Lambda, u)));
return psi;
}

dcomplex NIG_process_characteristic_exponent(dcomplex u, void *mod)
{
    return NIG_process_characteristic_exponent_without_cast(u, (NIG_process *) mod);
}

void NIG_process_update(NIG_process *process)
{
    process->Sigma = process->Delta;
    process->Theta = process->Beta * process->Delta * process->Delta;
    process->Nu = sqrt(process->Alpha * process->Alpha - process->Beta * process->Delta);

    process->Alpha_sqr = process->Alpha * process->Alpha;
    process->Sqrt_Alpha2_minus_Beta2 = sqrt(process->Alpha_sqr - process->Beta * process->Delta);
    process->Lambda = sqrt(process->Alpha_sqr - pow(process->Beta + 1, 2)) - process->Delta;
}

NIG_process *NIG_process_create(double Alpha, double Beta, double Delta, double Delta2)
{
    NIG_process *process = malloc(sizeof(NIG_process));
    process->Alpha = Alpha;
    process->Beta = Beta;
    process->Delta = Delta;
    process->nb_parameters = 3;
    NIG_process_update(process);

    //> Two way to compute drift term due to jump,
    //> Put on Band matrix
    (*jump_drift) = 0;
    //> Or Put in FD scheme (comment previous line and uncomment to next line)
    // (*jump_drift)= -process->C_Gamma_minus_Alpha_Minus*process->Lambdap1powAlphaMinus;
    //process->Lambdap1powAlphaMinus=0.0;
    return process;
};

```

```

NIG_process *NIG_process_create_from_vect(const PnlVect *input)
{
    int i;
    NIG_process *process = malloc(sizeof(NIG_process));
    process->nb_parameters = 3;
    for (i = 0; i < process->nb_parameters; i++)
        SETPROCESSPARAMETER(process, i, GET(input, i));
    NIG_process_update(process);
    return process;
};

```

```

NIG_process *NIG_process_create_from_brownian_time(double sigma_, double nu_, double theta_)
{
    double sigma_sqr = sigma_ * sigma_;
    NIG_process *process = malloc(sizeof(NIG_process));
    process->Theta = theta_;
    process->Sigma = sigma_;
    process->Nu = nu_;
    process->nb_parameters = 3;

    process->Alpha = sqrt(nu_ * nu_ / sigma_sqr + theta_ * theta_ / (sigma_sqr * sigma_sqr));
    process->Beta = theta_ / (sigma_sqr);
    process->Delta = sigma_;
    NIG_process_update(process);
    //>> Two way to compute drift term due to jump,
    //>> Put on Band matrix
    (*jump_drift) = 0;
    //>> Or Put in FD scheme (comment previous line and uncomment to next line)
    // (*jump_drift)= -process->C_Gamma_minus_Alpha_Minus*process->LambdapowAlphaMinus;
    //process->LambdapowAlphaMinus=0.0;
    return process;
};

```

```

void NIG_process_kill_drift(NIG_process *process)
{
    process->Lambda = 0.0;
};

void NIG_process_update_cast(void *process)
{
    NIG_process_update((NIG_process *)process);
}

```

```

}

// ----- VG -----

dcomplex VG_process_characteristic_exponent_without_cast(dcomplex u, VG_process
{
    //>> Case 1 code infinitesimal generator of backward k=i-j
    dcomplex psi = RCmul(mod->Kappa, C_op_amib(RCmul(mod->Sigma_srq_demi, Cmul(u,
    return RCmul(1 / mod->Kappa, C_op_amib(Clog(RCadd(1, psi)), RCmul(mod->Lambda,
}

dcomplex VG_process_characteristic_exponent(dcomplex u, void *mod)
{
    return VG_process_characteristic_exponent_without_cast(u, (VG_process *) mod);
}

void VG_process_update(VG_process *process)
{
    process->C = 1. / process->Kappa;
    process->G = sqrt(0.25 * process->Theta * process->Theta * process->Kappa * pr
    process->M = 1.0 / (process->G + 0.5 * process->Theta * process->Kappa);
    process->G = 1.0 / (process->G - 0.5 * process->Theta * process->Kappa);

    process->Sigma_srq_demi = process->Sigma * process->Sigma * 0.5;
    process->Lambda = log(1 - process->Kappa * (process->Sigma_srq_demi + process-
}
VG_process *VG_process_create(double Kappa, double Theta, double Sigma, double *
{
    VG_process *process = malloc(sizeof(VG_process));
    process->Kappa = Kappa;
    process->Theta = Theta;
    process->Sigma = Sigma;
    process->nb_parameters = 3;
    VG_process_update(process);
    //>> Two way to compute drift term due to jump,
    //>> Put on Band matrix
    (*jump_drift) = 0;
    //>> Or Put in FD scheme (comment previous line and uncomment to next line)
    // (*jump_drift)= -process->C_Gamma_minus_Alpha_Minus*process->LambdapowAlp
    //process->LambdapowAlphaMinus=0.0;

```

```

    return process;
};

VG_process *VG_process_create_from_vect(const PnlVect *input)
{
    int i;
    VG_process *process = malloc(sizeof(VG_process));
    process->nb_parameters = 3;
    for (i = 0; i < process->nb_parameters; i++)
        SETPROCESSPARAMETER(process, i, GET(input, i));
    VG_process_update(process);
    return process;
};

VG_process *VG_process_create_from_CGM(double C, double G, double M, double *jump)
{
    VG_process *process = malloc(sizeof(VG_process));
    process->C = C;
    process->G = G;
    process->M = M;
    process->nb_parameters = 3;

    process->Kappa = 1.0 / C;
    process->Theta = C / M - C / G;
    process->Sigma = sqrt(2 * C / (G * M));
    VG_process_update(process);
    //>> Two way to compute drift term due to jump,
    //>> Put on Band matrix
    (*jump_drift) = 0;
    //>> Or Put in FD scheme (comment previous line and uncomment to next line)
    // (*jump_drift)= -process->C_Gamma_minus_Alpha_Minus*process->Lambdap1powAlp
    //process->Lambdap1powAlphaMinus=0.0;
    return process;
};

void VG_process_kill_drift(VG_process *process)
{
    process->Lambda = 0.0;
};

```

```

void VG_process_update_cast(void *process)
{
    VG_process_update((VG_process *)process);
}

// ----- Meixner -----

dcomplex Meixner_process_characteristic_exponent_without_cast(dcomplex u, Meixner_process *process)
{
    //>> Case 1 code infinitesimal generator of backward k=i-j
    dcomplex psi = RCmul(0.5 * mod->Alpha, u);
    psi = Complex(psi.r, psi.i - 0.5 * mod->Beta);
    psi = Clog(RCmul(mod->cos_b2, Ccosh(psi)));
    return C_op_amib(RCmul(2 * mod->Delta, psi), RCmul(mod->Lambda, u));
}

dcomplex Meixner_process_characteristic_exponent(dcomplex u, void *mod)
{
    return Meixner_process_characteristic_exponent_without_cast(u, (Meixner_process *)mod);
}

void Meixner_process_update(Meixner_process *process)
{
    process->cos_b2 = 1.0 / cos(process->Beta * 0.5);
    process->Lambda = 2 * process->Delta * log((cos(0.5 * (process->Alpha + process->Beta))));
}

Meixner_process *Meixner_process_create(double Alpha, double Beta, double Delta,
{
    Meixner_process *process = malloc(sizeof(Meixner_process));
    process->Alpha = Alpha;
    process->Beta = Beta;
    process->Delta = Delta;
    process->nb_parameters = 3;
    Meixner_process_update(process);
    (*jump_drift) = 0;
    return process;
};

Meixner_process *Meixner_process_create_from_vect(const PnlVect *input)

```

```

{
    int i;
    Meixner_process *process = malloc(sizeof(Meixner_process));
    process->nb_parameters = 3;
    for (i = 0; i < process->nb_parameters; i++)
        SETPROCESSPARAMETER(process, i, GET(input, i));
    Meixner_process_update(process);
    return process;
};

void Meixner_process_update_cast(void *process)
{
    Meixner_process_update((Meixner_process *)process);
}

// ----- z_distribution -----

dcomplex z_distribution_process_characteristic_exponent_without_cast(dcomplex u,
{
    //>> Case 1 code infinitesimal generator of backward k=i-j
    //>> Case 1 code infinitesimal generator of backward k=i-j
    dcomplex psi = RCmul(0.5 * mod->Alpha, u);
    dcomplex psi2 = Complex(mod->Beta_2 - psi.i, psi.r);
    psi = Complex(mod->Beta_1 - psi.i, psi.r);
    psi = Clog(RCmul(mod->beta_b1_b2, Ctbeta(psi, psi2)));
    return C_op_amib(RCmul(-2 * mod->Delta, psi), RCmul(mod->Lambda, u));
}

dcomplex z_distribution_process_characteristic_exponent(dcomplex u, void *mod)
{
    return z_distribution_process_characteristic_exponent_without_cast(u, (z_distr
}

void z_distribution_process_update(z_distribution_process *process)
{
    process->beta_b1_b2 = 1.0 / tbeta(process->Beta_1, process->Beta_2);
    process->Lambda = 2 * process->Delta * log(tbeta(process->Beta_1 + 0.5 * M_1_P
}

```



```

z_distribution_process *z_distribution_process_create(double Alpha, double Beta_1, double Beta_2, double Delta, int *jump_drift)
{
    z_distribution_process *process = malloc(sizeof(z_distribution_process));
    process->Alpha = Alpha;
    process->Beta_1 = Beta_1;
    process->Beta_2 = Beta_2;
    process->Delta = Delta;
    process->nb_parameters = 4;
    z_distribution_process_update(process);
    (*jump_drift) = 0;
    return process;
};

z_distribution_process *z_distribution_process_create_from_vect(const PnlVect *input)
{
    int i;
    z_distribution_process *process = malloc(sizeof(z_distribution_process));
    process->nb_parameters = 3;
    for (i = 0; i < process->nb_parameters; i++)
        SETPROCESSPARAMETER(process, i, GET(input, i));
    z_distribution_process_update(process);
    return process;
};

void z_distribution_process_update_cast(void *process)
{
    z_distribution_process_update((z_distribution_process *)process);
}

// ----- Levy -----
dcomplex Levy_process_characteristic_exponent(dcomplex u, Levy_process *mod)
{
    return Csub(mod->characteristic_exponent(u, mod->process),
        Complex(mod->vol_square * (u.r * u.r - u.i * u.i + u.i), (mod->vol_square * u.i)));
}

dcomplex Levy_process_ln_characteristic_function(dcomplex u, double t, Levy_process *mod)
{
    return RCmul(-t, Levy_process_characteristic_exponent(u, mod));
}

```

```

}

dcomplex Levy_process_ln_characteristic_function_with_cast(dcomplex u, double t,
{
    return RCmul(-t, Levy_process_characteristic_exponent(u, (Levy_process *)mod))
}

dcomplex Levy_process_characteristic_function(dcomplex u, double t, Levy_process
{
    return Cexp(Levy_process_ln_characteristic_function(u, t, mod));
}

double Levy_process_get_sigma_square(Levy_process *Levy)
{
    return Levy->vol_square;
};

Levy_process *Levy_process_create(void *process_,
                                int nb_parameters_,
                                dcomplex(*characteristic_exponent_)(dcomplex
{
    Levy_process *Levy = malloc(sizeof(Levy_process));
    Levy->process = process_;
    Levy->nb_parameters = nb_parameters_;
    Levy->characteristic_exponent = characteristic_exponent_;
    Levy->update = update_;
    Levy->vol_square = IMPLICIT_VOL;
    return Levy;
};

Levy_process *Levy_process_create_from_vect(int model, const double *input)
{
    Levy_process *Levy = malloc(sizeof(Levy_process));
    PnlVect input_v;
    Levy->type_model = model;
    switch (model)
    {
        case 1:

```

```

    input_v = pnl_vect_wrap_array(input, 2);
    Levy->process = (void *)BS_process_create_from_vect(&input_v);
    Levy->nb_parameters = ((BS_process *) Levy->process)->nb_parameters;
    Levy->characteristic_exponent = BS_process_characteristic_exponent;
    break;
case 2:
    input_v = pnl_vect_wrap_array(input, 5);
    Levy->process = (void *)Merton_process_create_from_vect(&input_v);
    Levy->nb_parameters = ((Merton_process *) Levy->process)->nb_parameters;
    Levy->characteristic_exponent = Merton_process_characteristic_exponent;
    break;
case 3:
    input_v = pnl_vect_wrap_array(input, 4);
    Levy->process = (void *)CGMY_process_create_from_vect(&input_v);
    Levy->nb_parameters = ((CGMY_process *) Levy->process)->nb_parameters;
    Levy->characteristic_exponent = CGMY_process_characteristic_exponent;
    break;
case 4:
    input_v = pnl_vect_wrap_array(input, 6);
    Levy->process = (void *)Temperedstable_process_create_from_vect(&input_v);
    Levy->nb_parameters = ((Temperedstable_process *) Levy->process)->nb_param
    Levy->characteristic_exponent = Temperedstable_process_characteristic_expo
    break;
case 5:
    input_v = pnl_vect_wrap_array(input, 3);
    Levy->process = (void *)VG_process_create_from_vect(&input_v);
    Levy->nb_parameters = ((VG_process *) Levy->process)->nb_parameters;
    Levy->characteristic_exponent = VG_process_characteristic_exponent;
    break;
case 6:
    input_v = pnl_vect_wrap_array(input, 3);
    Levy->process = (void *)NIG_process_create_from_vect(&input_v);
    Levy->nb_parameters = ((NIG_process *) Levy->process)->nb_parameters;
    Levy->characteristic_exponent = NIG_process_characteristic_exponent;
    break;
case 7:
    input_v = pnl_vect_wrap_array(input, 3);
    Levy->process = (void *)Meixner_process_create_from_vect(&input_v);
    Levy->nb_parameters = ((Meixner_process *) Levy->process)->nb_parameters;
    Levy->characteristic_exponent = Meixner_process_characteristic_exponent;
    break;

```

```

    case 8:
        input_v = pnl_vect_wrap_array(input, 4);
        Levy->process = (void *)z_distribution_process_create_from_vect(&input_v);
        Levy->nb_parameters = ((z_distribution_process *) Levy->process)->nb_param
        Levy->characteristic_exponent = z_distribution_process_characteristic_expo
        break;
    default:
        return NULL;
    }
    Levy->vol_square = IMPLICIT_VOL;
    return Levy;
}

```

```

void Levy_process_free(Levy_process **Levy)
{
    switch ((*Levy)->type_model)
    {
        case 1:
            free((BS_process *)((*Levy)->process));
            break;
        case 2:
            free((BS_process *)((*Levy)->process));
            break;
        case 3:
            free((CGMY_process *)((*Levy)->process));
            break;
        case 4:
            free((Temperedstable_process *)((*Levy)->process));
            break;
        case 5:
            free((VG_process *)((*Levy)->process));
            break;
        case 6:
            free((NIG_process *)((*Levy)->process));
            break;
        case 7:
            free((Meixner_process *)((*Levy)->process));
            break;
        case 8:
            free((z_distribution_process *)((*Levy)->process));
            break;
    }
}

```

```

        default:
        {
            ;
        }
    }
    free(*Levy);
    *Levy = NULL;
};

void Levy_process_update(Levy_process *mod)
{
    mod->update(mod->process);
};

double Levy_process_get_parameter(Levy_process *mod, int i)
{
    GETLEVYPARAMETER(mod, i);
}

void Levy_process_set_parameter(Levy_process *mod, int i, double v)
{
    SETLEVYPARAMETER(mod, i, v);
}

void Levy_process_shift_parameter(Levy_process *mod, int i, int sg, double *shift)
{
    mod->initial_parameter = Levy_process_get_parameter(mod, i);
    ((double *)mod->process)[i] += sg * EPSILON_CALIBRATION; /*=(1+sg*EPSILON_CALIBRATION)*
    *shifted = EPSILON_CALIBRATION; //mod->initial_parameter*EPSILON_CALIBRATION;
    *shifted *= 2;
    Levy_process_update(mod);
}

void Levy_process_restore_parameter_without_restore(Levy_process *mod, int i)
{
    SETLEVYPARAMETER(mod, i, mod->initial_parameter);
}

void Levy_process_restore_parameter(Levy_process *mod, int i)
{
    Levy_process_restore_parameter_without_restore(mod, i);
    Levy_process_update(mod);
}

```

```

}

void Levy_process_print_parameter(Levy_process *mod)
{
    int i;
    for (i = 0; i < mod->nb_parameters; i++)
        printf("%7.4f, ", ((double *)mod->process)[i]);
    printf("\ n");
}

#undef GETPROCESSPARAMETER
#undef SETPROCESSPARAMETER
#undef GETLEVYPARAMETER
#undef SETLEVYPARAMETER

```