Help

```
#include <stdlib.h>
#include  "
href../../../mod/bs1d/bs1d_lim/bs1d_lim_h_src.pdfbs1d_lim.h"
#include "
href../../../common/error_msg_h_src.pdferror_msg.h"
#define PRECISION 1.0e-7 /*Precision for the localization of FD methods*/

static double initial_mesh(int upordown, double refinement, double x_min, double
{

  double atrois;
  double acinq;
  double temp;
  double x;
  double inref;

  inref = 1. / refinement;
  x = (x0 - x_min) / (x_max - x_min) - 0.5; /* t in [-0.5,0.5]*/
  temp = x;

  if (inref >= 0.2) /*inref > 0.17007... !).*/
    {
      if (upordown == 0)
        {
          acinq = 8 * (2.0 * inref + 1.0 / inref - 3.0);
          atrois = 2 * (5.0 - 4.0 * inref - 1.0 / inref);
          x = x / 2.0 + 0.25;
          temp = inref * x + atrois * x * x * x * x + acinq * x * x * x * x * x * x;
          temp = 2.0 * temp - 0.5;
        }
      else
        {
          acinq = 8.0 * (2.0 * inref + 1.0 / inref - 3.0);
          atrois = 2.0 * (5.0 - 4.0 * inref - 1.0 / inref);
          x = x / 2.0 - 0.25;
          temp = inref * x + atrois * x * x * x * x + acinq * x * x * x * x * x * x;
          temp = 2.0 * temp + 0.5;
        }
    }
```

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  return (temp + 0.5) * (x_max - x_min) + x_min;



}

static void new_mesh(double time, double *old_x, double z, double *new_x, int N)
{
  double new_x_min, new_x_max, rho;
  int i;

  new_x_min = old_x[0] + z * time;
  new_x_max = old_x[N] + z * time;
  rho = (new_x_max - new_x_min) / (old_x[N] - old_x[0]);

  for (i = 0; i <= N; i++)
    new_x[i] = new_x_min + rho * (old_x[i] - old_x[0]);

  return;
}

static int Fem_Out(int upordown, int am, double s, NumFunc_1  *p, NumFunc_1  *l,
{
  int      i, TimeIndex;
  double   vv, loc, h, z, V0, VN, A0, AN, Dir_low, Dir_up, Neu_low, Neu_up, sigm
  double   nu1, mu1, time_mesh, x_min, x_max, x0, nu_low, nu_up, mu_low, mu_up;
  double   *alpha, *beta, *gamma, *alpha1, *beta1, *gamma1, *old_x;
  double   *new_x, *V, *Vp, *beta_p, *P_New, *P_Old, *temp;

  /*Memory Allocation*/
  alpha = malloc((N + 1) * sizeof(double));
  if (alpha == NULL)
    return MEMORY_ALLOCATION_FAILURE;

  beta = malloc((N + 1) * sizeof(double));
  if (beta == NULL)
    return MEMORY_ALLOCATION_FAILURE;

  gamma = malloc((N + 1) * sizeof(double));
  if (gamma == NULL)
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  return MEMORY_ALLOCATION_FAILURE;

alpha1 = malloc((N + 1) * sizeof(double));
if (alpha1 == NULL)
  return MEMORY_ALLOCATION_FAILURE;

beta1 = malloc((N + 1) * sizeof(double));
if (beta1 == NULL)
  return MEMORY_ALLOCATION_FAILURE;

gamma1 = malloc((N + 1) * sizeof(double));
if (gamma1 == NULL)
  return MEMORY_ALLOCATION_FAILURE;

old_x = malloc((N + 1) * sizeof(double));
if (old_x == NULL)
  return MEMORY_ALLOCATION_FAILURE;

new_x = malloc((N + 1) * sizeof(double));
if (new_x == NULL)
  return MEMORY_ALLOCATION_FAILURE;

V = malloc((N + 1) * sizeof(double));
if (V == NULL)
  return MEMORY_ALLOCATION_FAILURE;

Vp = malloc((N + 1) * sizeof(double));
if (Vp == NULL)
  return MEMORY_ALLOCATION_FAILURE;

beta_p = malloc((N + 1) * sizeof(double));
if (beta_p == NULL)
  return MEMORY_ALLOCATION_FAILURE;

P_New = malloc((N + 1) * sizeof(double));
if (P_New == NULL)
  return MEMORY_ALLOCATION_FAILURE;

P_Old = malloc((N + 1) * sizeof(double));
if (P_Old == NULL)
  return MEMORY_ALLOCATION_FAILURE;
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temp = malloc((N + 1) * sizeof(double));
if (temp == NULL)
  return MEMORY_ALLOCATION_FAILURE;

/*Dirichlet on the barrier*/
nu1 = 0.;
mu1 = 1.;

/*Time Step*/
time_mesh = t / (double)M;

/*Space Localisation*/
sigma2 = sigma * sigma;
vv = 0.5 * sigma2;
z = (r - divid);

loc = sigma * sqrt(t) * sqrt(log(1.0 / PRECISION)) + fabs((z - vv) * t);
h = 0.001;

/*Terminal Values*/
if (upordown == 0) /*Down Case*/
  {
    x_min = log(((l->Compute)(l->Par, t)) / s) - z * t;
    x_max = loc;
  }
else/*Up Case*/
  {
    x_min = -loc;
    x_max = log(((l->Compute)(l->Par, t)) / s) - z * t;
  }

for (i = 0; i <= N; i++)
  {
    x0 = x_min + ((double)i) * (x_max - x_min) / (double)N;
    old_x[i] = initial_mesh(upordown, refinement, x_min, x_max, x0);
    P_Old[i] = exp(-r * t) * (p->Compute)(p->Par, s * exp(old_x[i] + z * t));
  }


if (upordown == 0) /*Down Case*/
```

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  P_Old[0] = exp(-r * t) * rebate;
else/*Up Case*/
  P_Old[N] = exp(-r * t) * rebate;

/*Finite Difference Cycle*/
for (TimeIndex = 1; TimeIndex <= M; TimeIndex++)
  {
    /*New Mesh Computing*/
    if (upordown == 0) /*Down Case*/
      {
        x_min = log(((l->Compute)(l->Par, t - (double)TimeIndex * time_mesh))
        x_max = loc;
      }
    else/*Up Case*/
      {
        x_min = -loc;
        x_max = log(((l->Compute)(l->Par, t - (double)TimeIndex * time_mesh))
      }
    /*New Mesh Generation*/
    new_mesh(time_mesh, old_x, z, new_x, N);

    /*Computation of Lhs coefficients*/
    for (i = 1; i < N; i++)
      {
        alpha[i] = (-vv * theta * time_mesh * (1. + 2.0 / (new_x[i] - new_x[i
                    - theta * (old_x[i - 1] - new_x[i - 1]));
        beta[i] = (new_x[i + 1] - new_x[i - 1]
                   + sigma2 * theta * time_mesh * (1.0 / (new_x[i + 1] - new_x
                       + 1.0 / (new_x[i] - new_x[i - 1])));
        gamma[i] = (vv * theta * time_mesh * (1. - 2.0 / (new_x[i + 1] - new_x
                    + theta * (old_x[i + 1] - new_x[i + 1]));
      }

    /*Computation of Rhs coefficients*/
    for (i = 1; i < N; i++)
      {
        alpha1[i] = (vv * (1.0 - theta) * time_mesh * (1. + 2.0 / (old_x[i] -
                     + (1.0 - theta) * (old_x[i - 1] - new_x[i - 1]));
        beta1[i] = (old_x[i + 1] - old_x[i - 1]
                    - sigma2 * (1.0 - theta) * time_mesh * (1.0 / (old_x[i + 1
                        + 1.0 / (old_x[i] - old_x[i - 1])));
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    gamma1[i] = (-vv * (1.0 - theta) * time_mesh * (1. - 2.0 / (old_x[i +
                - (1.0 - theta) * (old_x[i + 1] - new_x[i + 1]));
  }

/*Right factor*/
for (i = 1; i <= N - 1; i++)
  V[i] = alpha1[i] * P_Old[i - 1] + beta1[i] * P_Old[i] + gamma1[i] * P_Ol

/*Robin Boundary Condition in the Down Case*/
if (upordown == 0)
  {
    Dir_low = exp(-r * (t - (double)TimeIndex * time_mesh)) * rebate;
    Neu_low = 0.;
    nu_low = nu1;
    mu_low = mu1;



    V0 = (new_x[1] - new_x[0]) * (mu_low * Dir_low + nu_low * Neu_low) /
         (mu_low * (new_x[1] - new_x[0]) - nu_low);
    V[1] -= alpha[1] * V0; /*Robin low */
    A0 = nu_low / (mu_low * (new_x[1] - new_x[0]) - nu_low);
    beta[1] -= alpha[1] * A0;



    Dir_up = exp(-r * (t - (double)TimeIndex * time_mesh)) * (p->Compute)(

    /*Neumann condition is computed numerically*/
    Neu_up = exp(-r * (t - (double)TimeIndex * time_mesh)) * ((p->Compute)

    nu_up = nu2;
    mu_up = mu2;

    VN = (new_x[N] - new_x[N - 1]) * (mu_up * Dir_up + nu_up * Neu_up) /
         (mu_up * (new_x[N] - new_x[N - 1]) + nu_up);

    V[N - 1] -= gamma[N - 1] * VN; /*Robin up*/
    AN = -nu_up / (mu_up * (new_x[N] - new_x[N - 1]) + nu_up);
    beta[N - 1] -= gamma[N - 1] * AN;
  }
```

```
else /*Robin Boundary Condition in the Up Case*/
  {
    Dir_low = exp(-r * (t - (double)TimeIndex * time_mesh)) * (p->Compute)
    Neu_low = exp(-r * (t - (double)TimeIndex * time_mesh)) * ((p->Compute
    nu_low = nu2;
    mu_low = mu2;

    V0 = (new_x[1] - new_x[0]) * (mu_low * Dir_low + nu_low * Neu_low) /
         (mu_low * (new_x[1] - new_x[0]) - nu_low);
    V[1] -= alpha[1] * V0; /*Robin low */
    A0 = nu_low / (mu_low * (new_x[1] - new_x[0]) - nu_low);
    beta[1] -= alpha[1] * A0;

    Dir_up = exp(-r * (t - (double)TimeIndex * time_mesh)) * rebate;
    /*Neumann condition is computed numerically*/
    Neu_up = 0.;

    nu_up = nu1;
    mu_up = mu1;

    VN = (new_x[N] - new_x[N - 1]) * (mu_up * Dir_up + nu_up * Neu_up) /
         (mu_up * (new_x[N] - new_x[N - 1]) + nu_up);

    V[N - 1] -= gamma[N - 1] * VN; /*Robin up*/
    AN = -nu_up / (mu_up * (new_x[N] - new_x[N - 1]) + nu_up);
    beta[N - 1] -= gamma[N - 1] * AN;

  }

/*Gauss pivoting*/
Vp[N - 1] = V[N - 1];
beta_p[N - 1] = beta[N - 1];

for (i = N - 2; i >= 1; i--)
  {
    beta_p[i] = beta[i] - gamma[i] * alpha[i + 1] / beta_p[i + 1];
    Vp[i] = V[i] - gamma[i] * Vp[i + 1] / beta_p[i + 1];
  }
P_New[1] = Vp[1] / beta_p[1];
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```
    for (i = 2; i <= N - 1; i++)
      P_New[i] = (Vp[i] - alpha[i] * P_New[i - 1]) / beta_p[i];

    /*Splitting for the american case*/
    if (am)
      for (i = 1; i <= N - 1; i++)
        P_New[i] = MAX(P_New[i], exp(-r * (t - (double)TimeIndex * time_mesh))


    P_New[N] = VN - P_New[N - 1] * AN;
    P_New[0] = V0 - P_New[1] * A0;

    beta[1] += alpha[1] * A0;
    beta[N - 1] += gamma[N - 1] * AN;



    for (i = 0; i <= N; i++)
      {
        temp[i] = P_Old[i];
        P_Old[i] = P_New[i];
        P_New[i] = temp[i];
        temp[i] = old_x[i];
        old_x[i] = new_x[i];
        new_x[i] = temp[i];
      }

  }/*End of Time Cycle*/


i = 0;
while (old_x[i] < 0) i++;

/*Price*/
*ptprice = ((s - s * exp(old_x[i - 1])) * P_Old[i] + (s * exp(old_x[i]) - s) *
           (s * (exp(old_x[i]) - exp(old_x[i - 1])));

/*Delta*/
*ptdelta = (1.0 / (s * (s * (exp(old_x[i + 1]) - exp(old_x[i - 1]))))) * ((s *
```

```
  /*Memory Desallocation*/
  free(alpha);
  free(beta);
  free(gamma);
  free(alpha1);
  free(beta1);
  free(gamma1);
  free(old_x);
  free(new_x);
  free(V);
  free(Vp);
  free(beta_p);
  free(P_New);
  free(P_Old);
  free(temp);

  return OK;
}

int CALC(FD_Fem_Out)(void *Opt, void *Mod, PricingMethod *Met)
{
  TYPEOPT *ptOpt = (TYPEOPT *)Opt;
  TYPEMOD *ptMod = (TYPEMOD *)Mod;
  double r, divid, rebate;
  int upordown;

  r = log(1. + ptMod->R.Val.V_DOUBLE / 100.);
  divid = log(1. + ptMod->Divid.Val.V_DOUBLE / 100.);
  rebate = ((ptOpt->Rebate.Val.V_NUMFUNC_1)->Compute)((ptOpt->Rebate.Val.V_NUMFU
  if ((ptOpt->DownOrUp).Val.V_BOOL == DOWN)
    upordown = 0;
  else upordown = 1;

  return Fem_Out(upordown, ptOpt->EuOrAm.Val.V_BOOL, ptMod->S0.Val.V_PDOUBLE, pt
}

static int CHK_OPT(FD_Fem_Out)(void *Opt, void *Mod)
{
  Option *ptOpt = (Option *)Opt;
  TYPEOPT *opt = (TYPEOPT *)(ptOpt->TypeOpt);
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  if ((opt->OutOrIn).Val.V_BOOL == OUT)
    if ((opt->Parisian).Val.V_BOOL == FALSE)
      return OK;

  return  WRONG;
}

static int MET(Init)(PricingMethod *Met, Option *Opt)
{
  if (Met->init == 0)
    {
      Met->init = 1;
      Met->HelpFilenameHint = "fd_fem_out_bs";
      Met->Par[0].Val.V_INT2 = 100;
      Met->Par[1].Val.V_INT2 = 100;
      Met->Par[2].Val.V_RGDOUBLE = 0.5;
      Met->Par[3].Val.V_RGDOUBLE = 1.;
      Met->Par[4].Val.V_RGDOUBLE = 0.;
      Met->Par[5].Val.V_DOUBLE = 1.5;

    }

  return OK;
}

PricingMethod MET(FD_Fem_Out) =
{
  "FD_Fem_Out",
  { {"SpaceStepNumber", INT2, {100}, ALLOW    }, {"TimeStepNumber", INT2, {100},
    {"Theta", RGDOUBLE051, {100}, ALLOW}, {"Dirichlet Weights", RGDOUBLE, {100},
  },
  CALC(FD_Fem_Out),
  {{"Price", DOUBLE, {100}, FORBID}, {"Delta", DOUBLE, {100}, FORBID} , {" ", PR
  CHK_OPT(FD_Fem_Out),
  CHK_split,
  MET(Init)
};
```