

## [Help](#)

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extern "C" {
#include "
href../../mod/bmspectrally_negative1d/bmspectrally_negative1d_std/bmspectrally_n
#include "pnl/pnl_specfun.h"
#include "pnl/pnl_integration.h"
#include <pnl/pnl_complex.h>
}

typedef struct params_bmsntsl {
double C;
double G ;
double M;
double vol ;
double Y;
double r;
double mu;    // the drift fixed by the EMM requirement
double T;    // time to expiry
int N;        // the algorithm parameter: number of terms in the approximate formul
double K; //rebate
double S; //spot
double H; // barrier
    double x; // x-mu T
double alp; // parameter of the parabolic transform
double eps; // modified accuracy parameter epsilon_1 from the paper
double om; // the shift parameter
double d; // the algorithm parameter omega_alpha_f from the paper
double zet; // the space step in the approximate integral formula

} params_bmsntsl;

static void Set_params(params_bmsntsl *p, double r, double divid, double Sigma,
{

p->C = Cminus;    //in the paper C=c, Y=nu, G=lambda_+.
p->G = Lambdaminus; //lm=lambda_+
p->M = 20; //artificial lambda_-
p->vol = Sigma*Sigma / 2; //volatility
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p->Y = Alphaminus;
p->T = t;
p->N = N;
p->K = k;
p->S = s;
p->H = h;
p->r = r;
p->mu = r - p->vol - divid + pnl_sf_gamma(-Alphaminus)*Cminus*(exp(Alphaminus*log(s/h)+(p->mu)*t);
p->x = log(s/h)+(p->mu)*t;
p->alp = 1.4;
p->eps=M_PI*eps*exp(r*t);
if (p->x<0)//Call-like //
{
p->om=-0.4*p->M;
p->d = -p->M + pow(p->M, 1 - p->alp)*pow(p->M + 1.8*p->om, p->alp);
}
else // Put-like
{
p->om = 0.4*p->G;
p->d = p->G - pow(p->G, 1 - p->alp)*pow(p->G - 1.8*p->om, p->alp);
}
p->zet = 1.8*M_PI*p->om / (-log(p->eps) + p->mu*p->d*p->x - t*(-p->vol*p->d*p->d

}

static void psimTSL(params_bmsntsl *p, dcomplex u, dcomplex *res)//computation f
{
dcomplex aux1, aux2, aux3;

aux1 = RCmul(p->vol,Cmul(u, u));

aux2.r = p->G - u.i;
aux2.i = u.r;

aux3=Cexp(RCmul(p->Y,Clog(aux2)));

res->r = aux1.r+p->C*pnl_sf_gamma(-p->Y)*(exp(p->Y*log(p->G)) - aux3.r);
res->i = aux1.i-p->C*pnl_sf_gamma(-p->Y)*aux3.i;
}

static void psimTSLdrift(params_bmsntsl *p, dcomplex u, dcomplex *res)//computat

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{
dcomplex aux1, aux2, aux3, aux4;

aux1 = RCmul(p->vol, Cmul(u, u));

aux2.r = p->G - u.i;
aux2.i = u.r;

aux3 = Cexp(RCmul(p->Y, Clog(aux2)));

aux4.r = 0;
aux4.i = -p->mu;
aux4 = Cmul(aux4, u);

res->r = aux1.r + p->C*pn1_sf_gamma(-p->Y)*(exp(p->Y*log(p->G)) - aux3.r)+aux4.r;
res->i = aux1.i - p->C*pn1_sf_gamma(-p->Y)*aux3.i+aux4.i;
}

static dcomplex chip(double eta, double al, double om, double lp)
{
    dcomplex z, aux1, aux2, res;
    z.i=lp;
    z.r=0;
    aux1.i=eta;
    aux1.r=lp-om;
    aux2=Cexp(RCmul(al,Clog(aux1)));

    aux1.i=-pow(lp,1-al);
    aux1.r=0.;
    aux2=Cmul(aux1,aux2);
    res=Cadd(z,aux2);

    return res;
}

static dcomplex chim(double eta, double al, double om, double lm)// taken in the
                                                                    //"Efficient variati
//Journal of Computational Finance 18(2), 57-90
{
    dcomplex z, aux1, aux2, res;
    z.i=-lm;

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z.r=0;
aux1.i=-eta;
aux1.r=lm+om;
aux2=Cexp(RCmul(a1,Clog(aux1)));

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aux1.i=pow(lm-1.,1-a1);
aux1.r=0.;
aux2=Cmul(aux1,aux2);
res=Cadd(z,aux2);

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    return res;
}

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static dcomplex ZMueller(dcomplex beta, dcomplex q, double b1, double b2, void *

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params_bmsntsl *p = (params_bmsntsl*)pp;

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double d, d1, d2, x1, x2, x3, y1, y2, y3;
double u1, u2, u3, v1, v2, v3, xl1, xl2;
double a, a1, a2, b, c1, c2, e1, e2;
double e = 0.000001;
double x0, y0;
dcomplex aux, aux1, res;
int k;
int n = 1000; // the maximum number of iterations
// Start calculations
k = 0;
x3 = beta.r; y3 = beta.i;
x1 = x3 - b1; y1 = y3 - b2;
x2 = x3 + b1; y2 = y3 + b2;
res.r = beta.r; res.i = beta.i;

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do
{
k = k + 1; x0 = res.r; y0 = res.i;
d = (x2 - x1)*(x2 - x1) + (y2 - y1)*(y2 - y1);
// Avoid divide by zero
if (d == 0) d = 1e-7;
xl1 = (x3 - x2)*(x2 - x1) + (y3 - y2)*(y2 - y1);
xl1 = xl1 / d;
xl2 = (x2 - x1)*(y3 - y2) + (x3 - x2)*(y2 - y1);

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x12 = x12 / d;
d1 = (x3 - x1)*(x2 - x1) + (y3 - y1)*(y2 - y1);
d1 = d1 / d;
d2 = (x2 - x1)*(y3 - y1) + (x3 - x1)*(y2 - y1);
d2 = d2 / d;
// Get function values in 3 points
aux.r = x1;
aux.i = y1;
psimTSLdrift(p, aux, &aux1);
u1 = aux1.r + q.r; v1 = aux1.i + q.i;

aux.r = x2;
aux.i = y2;
psimTSLdrift(p, aux, &aux1);
u2 = aux1.r + q.r; v2 = aux1.i + q.i;

aux.r = x3;
aux.i = y3;
psimTSLdrift(p, aux, &aux1);
u3 = aux1.r + q.r; v3 = aux1.i + q.i;

// Calculate Mueller parameters
e1 = u1*(x11*x11 - x12*x12) - 2.0*v1*x11*x12 - u2*(d1*d1 - d2*d2);
e1 = e1 + 2.0*v2*d1*d2 + u3*(x11 + d1) - v3*(x12 + d2);
e2 = 2.0*x11*x12*u1 + v1*(x11*x11 - x12*x12) - 2.0*d1*d2*u2 - v2*(d1*d1 - d2*d2);
e2 = e2 + u3*(x12 + d2) + v3*(x11 + d1);
c1 = x11*x11*u1 - x11*x12*v1 - d1*x11*u2 + x11*d2*v2 + u3*x11;
c1 = c1 - u1*x12*x12 - v1*x11*x12 + u2*x12*d2 + v2*d1*x12 - v3*x12;
c2 = x11*x12*u1 + x11*x11*v1 - d2*x11*u2 - x11*d1*v2 + v3*x11;
c2 = c2 + u1*x11*x12 - v1*x12*x12 - u2*x12*d1 + v2*d2*x12 + u3*x12;
b1 = e1*e1 - e2*e2 - 4.0*(u3*d1*c1 - u3*d2*c2 - v3*d2*c1 - v3*d1*c2);
b2 = 2.0*e1*e2 - 4.0*(u3*d2*c1 + u3*d1*c2 + v3*d1*c1 - v3*d2*c2);
// Guard against divide by zero
if (b1 == 0) b1 = 1e-7;
a = atan(b2 / b1); a = a / 2.0;
b = sqrt(sqrt(b1*b1 + b2*b2));
b1 = b*cos(a); b2 = b*sin(a);
a1 = (e1 + b1)*(e1 + b1) + (e2 + b2)*(e2 + b2);
a2 = (e1 - b1)*(e1 - b1) + (e2 - b2)*(e2 - b2);

if (a1 > a2) { a1 = e1 + b1; a2 = e2 + b2; }

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else
{
a1 = e1 - b1; a2 = e2 - b2;
}
a = a1*a1 + a2*a2;
x11 = a1*d1*u3 - a1*d2*v3 + a2*u3*d2 + a2*v3*d1;
// Guard against divide by zero
if (a == 0) a = 1e-7;
x11 = -2.0*x11 / a;
x12 = -d1*u3*a2 + d2*v3*a2 + a1*u3*d2 + a1*v3*d1;
x12 = -2.0*x12 / a;
// Calculate new estimate
res.r = x3 + x11*(x3 - x2) - x12*(y3 - y2);
res.i = y3 + x12*(x3 - x2) + x11*(y3 - y2);

// Test for number of iterations
if (k >= n){ x0 = res.r; y0 = res.i; };
if (fabs(u3) + fabs(v3) < e){ res.r = x3; res.i = y3; x0 = res.r; y0 = res.i; }
// Test if beta_+ is negative
if (res.i >= 0){ res.i = -res.i - 20; }
// Continue
x1 = x2; y1 = y2; x2 = x3; y2 = y3; x3 = res.r; y3 = res.i;
} while (fabs(res.r - x0) + fabs(res.i - y0) > e);
return res;
} // ZMueller()

static double RePutInt(double eta, void *pp) ///Re( exp(ixChi_+(eta+i om)-T psi
{

params_bmsntsl *p = (params_bmsntsl*)pp;

dcomplex ix, aux, aux1, aux2, aux3, q, beta;

ix.i=p->x;
ix.r=0.;
//////////exponent computation//////////ok
aux=chip(eta,p->alp, p->om, p->G);
psimTSL(p, aux, &aux1);
aux2=Cmul(aux, ix);
aux1=CRmul(aux1,-p->T);

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aux1=Cadd(aux1,aux2);
//////////end//////////
//////////exp*G0 computation//////////
aux2 =Cdiv(Cexp(aux1),aux);
aux3.r=-aux2.i;
aux3.i = aux2.r;
psimTSLdrift(p, aux, &aux1);
aux3 =Cmul(aux3,aux1);
aux2 = CRadd(aux1, p->r);
aux3 = Cdiv(aux3, aux2);
//////////end//////////
////////// WH computation//////////
q.r = -aux1.r;
q.i = -aux1.i;
aux2 = Cexp(CRmul(Clog(CRdiv(q, p->vol)), 0.5));

beta.r = 0;
beta.i = -aux2.r; //guess approximate root of the equation q+psi(-ibeta_+)=0

beta = ZMueller(beta, q, 10, 1, p); //computation of beta=-ibeta_+ with the Muel
aux2.r = 0;
aux2.i = 1;
beta = Cmul(beta, aux2);/// beta_+///

aux2 = Cdiv(aux, beta);/// computation of
aux.r = 1 + aux2.i; /// beta_+(q) - i xi
aux.i = -aux2.r; /// -----
aux3 = Cmul(aux3, aux); /// beta_+(q)
//////////end//////////
//////////chi derivative computation//////////ok
aux.i=eta/(p->G);
aux.r=1-(p->om)/(p->G);
aux1=Cexp(RCmul(p->alp-1,Clog(aux)));
//////////end//////////
aux2=Cmul(aux3,aux1);
if (eta == p->N*p->zet){ aux2.r = 2.*aux2.r; }
return aux2.r*(p->alp);
}

static double ReCallInt(double eta, void *pp) ///Re( exp(ixChi_-(eta+i om)-T ps
{

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params_bmsntsl *p = (params_bmsntsl*)pp;

dcomplex ix, aux, aux1, aux2, aux3, q, beta;

ix.i=p->x;
ix.r=0.;
//////////exponent computation//////////ok
aux=chim(eta,p->alp, p->om, p->M);
psimTSL(p, aux, &aux1);
aux2=Cmul(aux, ix);
aux1=CRmul(aux1,-p->T);
aux1=Cadd(aux1,aux2);
//////////end//////////
//////////exp*G0 computation//////////
aux2 = Cdiv(Cexp(aux1), aux);
aux3.r = -aux2.i;
aux3.i = aux2.r;
psimTSLdrift(p, aux, &aux1);
aux3 = Cmul(aux3, aux1);
aux2 = CRadd(aux1, p->r);
aux3 = Cdiv(aux3, aux2);
//////////end//////////
////////// WH computation//////////
q.r = -aux1.r;
q.i = -aux1.i;
aux2 = Cexp(CRmul(Clog(CRdiv(q, p->vol)), 0.5));

beta.r = 0;
beta.i = -aux2.r; //guess approximate root of the equation q+psi(-ibeta_+)=0

beta = ZMueller(beta, q, 10, 1, p); //computation of beta=-ibeta_+ with the Muel
aux2.r = 0;
aux2.i = 1;
beta = Cmul(beta, aux2);/// beta_+///

aux2 = Cdiv(aux, beta);/// computation of
aux.r = 1 + aux2.i; /// beta_+(q) - i xi
aux.i = -aux2.r; /// -----
aux3 = Cmul(aux3, aux); /// beta_+(q)
//////////end//////////

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//////////chi derivative computation//////////
aux.i=-eta/(p->M-1);
aux.r=(p->M+p->om)/(p->M-1);
aux1=Cexp(RCmul(p->alp-1,Clog(aux)));
//////////end//////////
aux2=Cmul(aux3,aux1);
if (eta == p->N*p->zet){ aux2.r = 2.*aux2.r; }
return aux2.r*(p->alp);
}

extern "C" {
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2018+2) //The "#els
    static int CHK_OPT(AP_Levendorskii)(void *Opt, void *Mod)
    {
        return NONACTIVE;
    }
    int CALC(AP_Levendorskii)(void *Opt, void *Mod, PricingMethod *Met)
    {
        return AVAILABLE_IN_FULL_PREMIA;
    }
#else

    static int Levendorskii(double Spot,double rebate, NumFunc_1 *payoff, double
    {
        double Strike;
        Strike = payoff->Par[0].Val.V_DOUBLE;
params_bmsnts1 p;
double eps;
double UP_PARFT;
PnlFunc Put, Call;

eps = 0.0005;//Accuracy

Set_params(&p, r, divid, Sigma, Alphaminus, Lambdaminus, Cminus, T, rebate, Spot
if (p.S>p.H)// the barrier is not crossed
    {
if (p.x>0)
{
UP_PARFT = p.N*p.zet;
Put.F = &RePutInt;

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Put.params = &p;
*ptprice = pnl_integration (&Put, 0, UP_PARFT, p.N , "trap");
*ptprice = *ptprice*p.K/M_PI;
}
else {
UP_PARFT = p.N*p.zet;
Call.F = &ReCallInt;
Call.params = &p;
*ptprice = pnl_integration (&Call, 0, UP_PARFT, p.N , "trap");
*ptprice = *ptprice*p.K/M_PI;
}
*ptprice = exp(-r*T)**ptprice;
}
else // the barrier is already crossed
{
*ptprice = p.K;
//printf("The barrier is already crossed. Please increase the spot price. \n");
}
return OK;
}

int CALC(AP_Levendorskii)(void *Opt, void *Mod, PricingMethod *Met)
{
TYPEOPT *ptOpt = (TYPEOPT *)Opt;
TYPEMOD *ptMod = (TYPEMOD *)Mod;
double r, divid;
double rebate;
NumFunc_1 *p;

r = log(1. + ptMod->R.Val.V_DOUBLE / 100.);
divid = log(1. + ptMod->Divid.Val.V_DOUBLE / 100.);
p = ptOpt->PayOff.Val.V_NUMFUNC_1;
rebate = p->Par[1].Val.V_DOUBLE;

return Levendorskii(ptMod->S0.Val.V_PDOUBLE, rebate, ptOpt->PayOff.Val.V_NUMFU
}

static int CHK_OPT(AP_Levendorskii)(void *Opt, void *Mod)
{
if ((strcmp(((Option *)Opt)->Name, "DigitAmer") == 0))
return OK;
}

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    return WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met, Option *Opt)
{
    static int first = 1;

    if (first)
    {
        Met->Par[0].Val.V_PINT = 12 ;
        first = 0;
    }

    return OK;
}

PricingMethod MET(AP_Levendorskii) =
{
    "AP_Levendorskii",
    {"Number of Space Steps", PINT, {100}, ALLOW    },
{" " , PREMIA_NULLTYPE, {0}, FORBID}},
    CALC(AP_Levendorskii),
    {"Price", DOUBLE, {100}, FORBID}, {" " , PREMIA_NULLTYPE, {0}, FORBID}},
    CHK_OPT(AP_Levendorskii),
    CHK_ok,
    MET(Init)
} ;
}

```