

## cf\_floating\_calllookback

Let

- $T$  = maturity date ( $T > t$ )
- $x$  = spot price
- $m$  = current minimum  $m_{0,t}$
- $t$  = pricing date
- $\sigma$  = volatility
- $r$  = interest rate
- $\delta$  = dividend yields
- $\theta = T - t$
- $b = r - \delta$

Floating strike lookback options can be priced using Goldman-Sosin-Gatto formula [1] while fixed strike lookback options can be priced using Conze-Viswanathen formula[2].

We set, as  $0 \leq u \leq v \leq T$ ,

$$M_{u,v} = \sup_{u \leq \tau \leq v} S_\tau \quad \text{and} \quad m_{u,v} = \inf_{u \leq \tau \leq v} S_\tau$$

and

$$\begin{aligned}
 \bullet \quad d_1 &= \frac{\log\left(\frac{x}{K}\right) + \left(b + \frac{\sigma^2}{2}\right)\theta}{\sigma\sqrt{\theta}} & d_2 &= d_1 - \sigma\sqrt{\theta} \\
 \bullet \quad e_1 &= \frac{\log\left(\frac{x}{M_{0,t}}\right) + \left(b + \frac{\sigma^2}{2}\right)\theta}{\sigma\sqrt{\theta}} & e_2 &= e_1 - \sigma\sqrt{\theta} \\
 \bullet \quad f_1 &= \frac{\log\left(\frac{x}{m_{0,t}}\right) + \left(b + \frac{\sigma^2}{2}\right)\theta}{\sigma\sqrt{\theta}} & f_2 &= f_1 - \sigma\sqrt{\theta}
 \end{aligned}$$

# Floatin Lookback Call Option

PAYOFF	$C_T = S_T - m_{t,T}$
PRICE	$C(t, x) = xe^{-\delta\theta}N(f_1) - m_{0,t}e^{-r\theta}N(f_2)$ $+xe^{-r\theta}\frac{\sigma^2}{2b}\left[\left(\frac{x}{m_{0,t}}\right)^{-\frac{2b}{\sigma^2}}N\left(-f_1 + \frac{2b}{\sigma}\sqrt{\theta}\right) - e^{b\theta}N(-f_1)\right]$
DELTA	$\frac{\partial C(t, x)}{\partial x} = e^{-\delta\theta}N(f_1)\left(1 + \frac{\sigma^2}{2b}\right) + e^{-\delta\theta}\frac{n(a_1)}{\sigma\sqrt{\theta}}$ $-e^{-r\theta}\frac{\sigma^2}{2b} + e^{-r\theta}\left(\frac{x}{m_{0,t}}\right)^{-\frac{2b}{\sigma^2}}N\left(-f_1 + \frac{2b}{\sigma}\sqrt{t}\right)\left(\frac{\sigma^2}{2b} - 1\right)$

## References

- [1] B.M.GOLDMAN H.B.SOSIN M.A.GATTO. Path dependent options: buy at low, sell at high. *J. of Finance*, 34:111–127, 1979. [1](#)
- [2] A.CONZE R.VISWANATHAN. Path dependent options: the case of lookback options. *J. of Finance*, 46:1893–1907, 1992. [1](#)