

[Help](#)

```
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2008+2) //The "#els
#else

#include "
href../../common/math/alfonsi_h_src.pdfalfonsi.h"

double psik(double t, double k)
{
    if (k == 0.) return t;
    return (1 - exp(-k * t)) / k;
}

double DiscLawMatch5(int generator)
{
    double u = pnl_rand_uni(generator);
    if (u < 1. / 6.) return -sqrt(3);
    if (u < 1. / 3.) return sqrt(3);
    return 0;
}

double DiscLawMatch7(int generator)
{
    double u = 2.*pnl_rand_uni(generator) - 1.;
    double res = sqrt(6);
    if (fabs(u) < ((res - 2) / (2 * res))) res = sqrt(3 + res);
    else res = sqrt(3 - res);
    if (u < 0) return -res;
    return res;
}

static double O3_1(double t, double x, double a, double k, double sig)
{
    double aux;

    if (k == 0) aux = t;
    else aux = (1 - exp(-k * t)) / k;
    return x * exp(-k * t) + (a - 0.25 * sig * sig) * aux;
}
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}

static double O3_2(double t, double x, double sig)
{
    double aux = MAX(sqrt(x) + 0.5 * sig * t, 0);
    return SQR(aux);
}

static double O3_3(double t, double x, double a, double k, double sig, int ordre)
{
    double aux = (a - 0.25 * sig * sig + k * x) * 0.5 * sig * sig;

    if (aux > 0) return x + sqrt(aux) * t + k * sig * sig * 0.125 * t * t;
    if (aux < 0) return x + sqrt(-aux) * t - k * sig * sig * 0.125 * t * t;
    return x;
}

void Heston01(double *x1, double *x2, double *x3, double *x4, double dt, double
              double a, double k, double sig, double mu, double rho, double Kseu)
{
    double dx = 0., aux, ratio, p;
    double sig2 = SQR(sig);
    double pp, ee;
    double u1, u2, u3;
    double s, res, dt2, dw2;
    int ordre;
    double rd = 0;

    if (flag_cir == 1)
    {
        if (*x1 > Kseuil * dt)
        {
            aux = exp(-k * 0.5 * dt);
            if (k == 0.)
                u1 = (a - SQR(0.5 * sig)) * dt * 0.5;
            else u1 = (a - SQR(0.5 * sig)) * (1 - aux) / k;
            dx = MAX(aux * SQR(sqrt(u1 + aux * (*x1))) + 0.5 * sig * dw) + u1 - *x1;
        }
        else
        {
            aux = exp(-k * dt);

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    u1 = (*x1) * aux + a * (1 - aux) / k;
    ratio = (SQR(*x1 * aux) + (2 * a + sig * sig) * (((1 - aux * aux) / (2 *
    p = 0.5 * (1 - sqrt(1 - 1 / ratio)));

    if (pnl_rand_uni(generator) < p) dx = u1 / (2 * p) - *x1;
    else dx = u1 / (2 * (1 - p)) - *x1;
}
}
else if (flag_cir == 2)
{
    if (*x1 < Kseuil * dt)
    {
        ee = exp(-k * dt);
        if (k == 0.) pp = dt;
        else pp = (1 - ee) / k;
        u1 = *x1 * ee + a * pp;
        u2 = u1 * u1 + sig2 * pp * (0.5 * a * pp + *x1 * ee);
        u3 = u1 * u2 + sig2 * pp * (2 * *x1 **x1 * ee * ee + pp * (a + 0.5 * s
        s = (u3 - u1 * u2) / (u2 - u1 * u1);
        p = (u1 * u3 - u2 * u2) / (u2 - u1 * u1);
        p = sqrt(s * s - 4 * p);
        u2 = 0.5 * (s - p);
        u3 = u2 + p;

        if (pnl_rand_uni(generator) < (u1 - u2) / (u3 - u2)) dx = u3 - *x1;
        else dx = u2 - *x1;
    }
    else
    {
        if (a - 0.25 * sig2 > 0) ordre = 1;
        else ordre = 0;
        // On intègre 2

        if (k == 0.) dt2 = dt;
        else dt2 = (exp(k * dt) - 1) / k;
        dw2 = sqrt(dt2 / dt) * dw;

        // else ordre=-1;

        rd = 3 * pnl_rand_uni(generator);
        if (rd < 1)

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{
    if (rd < 0.5) s = -1;
    else s = 1;
    if (ordre == 1)
    {
        res = 03_3(s * dt2, *x1, a, 0, sig, ordre);
        res = 03_2(dw2, res, sig);
        res = 03_1(dt2, res, a, 0, sig);
    }
    else
    {
        res = 03_3(s * dt2, *x1, a, 0, sig, ordre);
        res = 03_1(dt2, res, a, 0, sig);
        res = 03_2(dw2, res, sig);
    }

    dx = exp(-k * dt) * res - *x1;
}
else
{
    if (rd < 2)
    {
        if (rd - 1 < 0.5) s = -1;
        else s = 1;
        if (ordre == 1)
        {
            res = 03_2(dw2, *x1, sig);
            res = 03_3(s * dt2, res, a, 0, sig, ordre);
            res = 03_1(dt2, res, a, 0, sig);
        }
        else
        {
            res = 03_1(dt2, *x1, a, 0, sig);
            res = 03_3(s * dt2, res, a, 0, sig, ordre);
            res = 03_2(dw2, res, sig);
        }
        dx = exp(-k * dt) * res - *x1;
    }
    else if (rd >= 2.)
    {
        if (rd - 2. < 0.5) s = -1;

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        else s = 1;
        if (ordre == 1)
        {
            res = O3_2(dw2, *x1, sig);
            res = O3_1(dt2, res, a, 0, sig);
            res = O3_3(s * dt2, res, a, 0, sig, ordre);
        }
        else
        {
            res = O3_1(dt2, *x1, a, 0, sig);
            res = O3_2(dw2, res, sig);
            res = O3_3(s * dt2, res, a, 0, sig, ordre);
        }

        dx = exp(-k * dt) * res - *x1;
    }
}

}

*x2 = *x2 + (*x1 + 0.5 * dx) * dt;
*x4 = *x4 + 0.5 * (*x3) * dt;
*x3 = *x3 * exp((mu - rho * a / sig) * dt + rho * dx / sig + (rho * k / sig -
*x4 = *x4 + 0.5 * (*x3) * dt;
*x1 = *x1 + dx;

return;
}

void Heston02(double *x1, double *x3, double dw2, double rho)
{
    *x3 = (*x3) * exp(sqrt((1 - rho * rho) * (*x1)) * dw2);

    return;
}

void fct_Heston(double *x1, double *x2, double *x3, double *x4, double dt, doubl
{
    if (pnl_rand_uni(generator) > 0.5)
    {
        Heston02(x1, x3, dw2, rho);
    }
}

```

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        Heston01(x1, x2, x3, x4, dt, dw, a, k, sig, mu, rho, Kseuil, generator,
    }
else
{
    Heston01(x1, x2, x3, x4, dt, dw, a, k, sig, mu, rho, Kseuil, generator,
    Heston02(x1, x3, dw2, rho);
}
return;
}

```

```

/** Simulation of the Heston model, using the method proposed by Aurélien Alfonsi
* @param flag_SpotPaths flag to decides whether to store SpotPaths or not.
* @param SpotPaths will contain the paths simulation of the spot
* @param flag_VarPaths flag to decides whether to store VarPaths or not.
* @param VarPaths will contain the paths simulation of the variance
* @param flag_AveragePaths flag to decides whether to store AveragePaths or not.
* @param AveragePaths will contain the paths simulation of the average of spot.
* @param S0 initial value of the spot.
* @param T last date in the simulation.
* @param r interest rate, divid dividend rate.
* @param V0, k, theta, sigma and rho: Heston parameters (Initial variance, mean
* @param NbrMCsimulation number of simulated paths
* @param NbrDates number of sample in each path to be stored in SpotPaths and Va
* @param NbrStepPerPeriod number of steps of discretization between T(i) and T(i
* @param generator the index of the random generator to be used
* @param flag_cir parameter of Alfonsi's method
*/
int HestonSimulation_Alfonsi(int flag_SpotPaths, PnlMat *SpotPaths, int flag_Var
{
    long i, j, m;
    double g1, g2, h, sqrt_h, w_t_1, w_t_2, aaa, Kseuil, aux, mu, t;

    double X1a, X2a, X3a, X4a;

    h = T / (double)((NbrDates - 1) * NbrStepPerPeriod);
    sqrt_h = sqrt(h);
    aaa = k * theta;
    mu = r - divid;

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if (flag_cir == 1)
    Kseuil = MAX((0.25 * SQR(sigma) - aaa) * psik(h * 0.5, k), 0.);
else
{
    if (k == 0)
        Kseuil = 1;
    else Kseuil = (exp(k * h) - 1) / (h * k);
    if (sigma * sigma <= 4 * k * theta / 3)
    {

        Kseuil = Kseuil * sigma * sqrt(k * theta - sigma * sigma / 4) / sqrt(2)
    }
    if (sigma * sigma > 4 * k * theta / 3 && sigma * sigma <= 4 * k * theta)
    {
        aux = (0.5 * sigma * sqrt(3 + sqrt(6)) + sqrt(sigma * sigma / 4 - k *
        Kseuil = Kseuil * SQR(aux);
    }
    if (sigma * sigma > 4 * k * theta)
    {
        aux = 0.5 * sigma * sqrt(3 + sqrt(6)) + sqrt(sigma * sqrt(sigma * sigma
        Kseuil = Kseuil * (sigma * sigma / 4 - k * theta + SQR(aux));
    }
    if (sigma * sigma == 4 * k * theta) Kseuil = 0;
}

if (flag_SpotPaths == 1) pnl_mat_resize(SpotPaths, NbrDates, NbrMCsimulation);
if (flag_VarPaths == 1) pnl_mat_resize(VarPaths, NbrDates, NbrMCsimulation);
if (flag_AveragePaths == 1) pnl_mat_resize(AveragePaths, NbrDates, NbrMCsimulation);

for (m = 0; m < NbrMCsimulation; m++)
{
    /* Begin of the N iterations */
    t = 0.;
    X1a = V0; // X1a: Variance
    X2a = 0; // X2a: Integral of Variance
    X3a = S0; // X3a: Spot
    X4a = 0; // X4a: Integral of Spot

    if (flag_VarPaths == 1) MLET(VarPaths, 0, m) = X1a;
    if (flag_SpotPaths == 1) MLET(SpotPaths, 0, m) = X3a;
    if (flag_AveragePaths == 1) MLET(AveragePaths, 0, m) = X3a; // at time 0,

```

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for (i = 1 ; i <= NbrDates - 1 ; i++)
{
    for (j = 0 ; j < NbrStepPerPeriod; j++)
    {
        t += h;
        /*Discrete law obtained by matching of first
        five moments of a gaussian r.v.*/
        if (flag_cir == 1)
            g1 = DiscLawMatch5(generator);
        else
            g1 = DiscLawMatch7(generator);
        w_t_1 = sqrt_h * g1;

        g2 = pnl_rand_normal(generator);
        w_t_2 = sqrt_h * g2;

        fct_Heston(&X1a, &X2a, &X3a, &X4a, h, w_t_1, w_t_2, aaa, k, sigma,
        }

        if (flag_VarPaths == 1) MLET(VarPaths, i, m) = X1a;
        if (flag_SpotPaths == 1) MLET(SpotPaths, i, m) = X3a;
        if (flag_AveragePaths == 1) MLET(AveragePaths, i, m) = X4a / t;
    }

}

/* End of the NbrMCsimulation iterations */
return OK;
}

```

```

/** Simulation of the Bates model, using the method proposed by Aurélien Alfonsi
* @param flag_SpotPaths flag to decides whether to store SpotPaths or not.
* @param SpotPaths will contain the paths simulation of the spot
* @param flag_VarPaths flag to decides whether to store VarPaths or not.
* @param VarPaths will contain the paths simulation of the variance
* @param flag_AveragePaths flag to decides whether to store AveragePaths or not.
* @param AveragePaths will contain the paths simulation of the average of spot.
* @param S0 initial value of the spot.
* @param T last date in the simulation.
* @param r interest rate, divid dividend rate.

```



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* @param V0, k, theta, sigma, rho, mu_jump, gamma2 and lambda,: Bates parameters
* @param NbrMCsimulation number of simulated paths
* @param NbrDates number of sample in each path to be stored in SpotPaths and Va
* @param NbrStepPerPeriod number of steps of discretization between T(i) and T(i+1)
* @param generator the index of the random generator to be used
* @param flag_cir parameter of Alfonsi's method
*/
int BatesSimulation_Alfonsi(int flag_SpotPaths, PnlMat *SpotPaths, int flag_VarP
{
    int i, j;
    long m;
    double g1, g2;
    double t_i, h, sqrt_h;
    double X1a, X2a, X3a, X4a;
    double w_t_1, w_t_2;
    double aaa, Kseuil, aux, mu;
    double prev_jump, next_jump, h2, sqrt_h2, jump, correction_mg, mu2, sg_jump;

    h = T / (double)((NbrDates - 1) * NbrStepPerPeriod);
    sqrt_h = sqrt(h);
    aaa = k * theta;
    mu = r - divid;
    prev_jump = 0;

    sg_jump = sqrt(gamma2);
    correction_mg = lambda * (exp(mu_jump + 0.5 * gamma2) - 1);
    mu2 = mu - correction_mg;
    if (flag_cir == 1)
        Kseuil = MAX((0.25 * SQR(sigma) - aaa) * psik(h * 0.5, k), 0.);
    else
    {
        if (k == 0)
            Kseuil = 1;
        else Kseuil = (exp(k * h) - 1) / (h * k);
        if (sigma * sigma <= 4 * k * theta / 3)
        {
            Kseuil = Kseuil * sigma * sqrt(k * theta - sigma * sigma / 4) / sqrt(2)
        }
        if (sigma * sigma > 4 * k * theta / 3 && sigma * sigma <= 4 * k * theta)
        {

```

```

        aux = (0.5 * sigma * sqrt(3 + sqrt(6)) + sqrt(sigma * sigma / 4 - k *
        Kseuil = Kseuil * SQR(aux);
    }
    if (sigma * sigma > 4 * k * theta)
    {
        aux = 0.5 * sigma * sqrt(3 + sqrt(6)) + sqrt(sigma * sqrt(sigma * sigma
        Kseuil = Kseuil * (sigma * sigma / 4 - k * theta + SQR(aux));
    }
    if (sigma * sigma == 4 * k * theta) Kseuil = 0;
}

if (flag_SpotPaths == 1) pnl_mat_resize(SpotPaths, NbrDates, NbrMCsimulation);
if (flag_VarPaths == 1) pnl_mat_resize(VarPaths, NbrDates, NbrMCsimulation);
if (flag_AveragePaths == 1) pnl_mat_resize(AveragePaths, NbrDates, NbrMCsimulation);

for (m = 0; m < NbrMCsimulation; m++)
{
    /* Begin of the N iterations */
    t_i = 0.;
    X1a = V0; // X1a: Volatility
    X2a = 0; // X1a: Integral of Volatility
    X3a = S0; // X1a: Spot
    X4a = 0; // X1a: Integral of Spot

    if (flag_VarPaths == 1) MLET(VarPaths, 0, m) = X1a;
    if (flag_SpotPaths == 1) MLET(SpotPaths, 0, m) = X3a;
    if (flag_AveragePaths == 1) MLET(AveragePaths, 0, m) = X3a; // at time 0,

    next_jump = -log(pnl_rand_uni(generator)) / lambda;

    for (i = 1 ; i <= NbrDates - 1 ; i++)
    {
        for (j = 0 ; j < NbrStepPerPeriod; j++)
        {
            t_i += h;

            /*Discrete law obtained by matching of first five moments of a gaussian
            if (next_jump > t_i)
            {
                if (flag_cir == 1)
                    g1 = DiscLawMatch5(generator);
            }
        }
    }
}

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else
    g1 = DiscLawMatch7(generator);
    w_t_1 = sqrt_h * g1;

    g2 = pnl_rand_normal(generator);
    w_t_2 = sqrt_h * g2;

    fct_Heston(&X1a, &X2a, &X3a, &X4a, h, w_t_1, w_t_2, aaa, k, si
}
else
{
    h2 = next_jump - (t_i - h);
    sqrt_h2 = sqrt(h2);

    while (next_jump <= t_i)
    {

        if (flag_cir == 1)
            g1 = DiscLawMatch5(generator);
        else
            g1 = DiscLawMatch7(generator);
        w_t_1 = sqrt_h2 * g1;

        g2 = pnl_rand_normal(generator);
        w_t_2 = sqrt_h2 * g2;
        fct_Heston(&X1a, &X2a, &X3a, &X4a, h2, w_t_1, w_t_2, aaa,
        prev_jump = next_jump;
        next_jump = next_jump - log(pnl_rand_uni(generator)) / lam
        h2 = next_jump - prev_jump;
        sqrt_h2 = sqrt(h2);
        jump = exp(mu_jump + sg_jump * pnl_rand_normal(generator))
        X3a = X3a * jump;
    }

    h2 = t_i - prev_jump;
    sqrt_h2 = sqrt(h2);

    if (flag_cir == 1)
        g1 = DiscLawMatch5(generator);
    else

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* @param V0, k, theta, sigma and rho: Heston parameters (Initial variance, mean
* @param NbrMCsimulation number of simulated paths
* @param NbrDates number of sample in each path to be stored in SpotPaths and Va
* @param NbrStepPerPeriod number of steps of discretization between T(i) and T(i
* @param generator the index of the random generator to be used
* @param flag_cir parameter of Alfonsi's method
*/

int HestonSimulation_Alfonsi_Modified(int flag_SpotPaths, PnlMat *SpotPaths, int
{
    long i, j, m;
    double g1, g2, h, sqrt_h, w_t_1, w_t_2, aaa, Kseuil, aux, mu, t;

    double X1a, X2a, X3a, X4a;

    h = T / (double)((NbrDates - 1) * NbrStepPerPeriod);
    sqrt_h = sqrt(h);
    aaa = k * theta;
    mu = r - divid;

    if (flag_cir == 1)
        Kseuil = MAX((0.25 * SQR(sigma) - aaa) * psik(h * 0.5, k), 0.);
    else
    {
        if (k == 0)
            Kseuil = 1;
        else Kseuil = (exp(k * h) - 1) / (h * k);
        if (sigma * sigma <= 4 * k * theta / 3)
        {
            Kseuil = Kseuil * sigma * sqrt(k * theta - sigma * sigma / 4) / sqrt(2)
        }
        if (sigma * sigma > 4 * k * theta / 3 && sigma * sigma <= 4 * k * theta)
        {
            aux = (0.5 * sigma * sqrt(3 + sqrt(6)) + sqrt(sigma * sigma / 4 - k *
            Kseuil = Kseuil * SQR(aux);
        }
        if (sigma * sigma > 4 * k * theta)
        {
            aux = 0.5 * sigma * sqrt(3 + sqrt(6)) + sqrt(sigma * sqrt(sigma * sigma
            Kseuil = Kseuil * (sigma * sigma / 4 - k * theta + SQR(aux));
        }
    }
}

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    }
    if (sigma * sigma == 4 * k * theta) Kseuil = 0;
}

// No need to resize in this version, indeed, the size is already fixed
// in the principal function MalliavinImproved_Heston.
//if(flag_SpotPaths==1) pnl_mat_resize(SpotPaths, NbrDates, NbrMCsimulation);
//if(flag_VarPaths==1) pnl_mat_resize(VarPaths, NbrDates, NbrMCsimulation);
//pnl_mat_resize(VarianceInt, NbrDates, NbrMCsimulation);
if (flag_AveragePaths == 1) pnl_mat_resize(AveragePaths, NbrDates, NbrMCsimulation);

for (m = 0; m < NbrMCsimulation; m++)
{
    // Begin of the N iterations
    t = 0.;
    X1a = V0; // X1a: Variance
    X2a = 0; // X2a: Integral of Variance
    X3a = S0; // X3a: Spot
    X4a = 0; // X4a: Integral of Spot

    if (flag_VarPaths == 1) MLET(VarPaths, 0, m) = X1a;
    if (flag_SpotPaths == 1) MLET(SpotPaths, 0, m) = X3a;
    if (flag_AveragePaths == 1) MLET(AveragePaths, 0, m) = X3a; // at time 0,
    MLET(VarianceInt, 0, m) = X2a;

    for (i = 1 ; i <= NbrDates - 1 ; i++)
    {
        for (j = 0 ; j < NbrStepPerPeriod; j++)
        {
            t += h;
            //Discrete law obtained by matching of first
            //five moments of a gaussian r.v.
            if (flag_cir == 1)
                g1 = DiscLawMatch5(generator);
            else
                g1 = DiscLawMatch7(generator);
            w_t_1 = sqrt_h * g1;

            g2 = pnl_rand_normal(generator);

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        w_t_2 = sqrt_h * g2;

        fct_Heston(&X1a, &X2a, &X3a, &X4a, h, w_t_1, w_t_2, aaa, k, sigma,
    }

    if (flag_VarPaths == 1) MLET(VarPaths, i, m) = X1a;
    if (flag_SpotPaths == 1) MLET(SpotPaths, i, m) = X3a;
    if (flag_AveragePaths == 1) MLET(AveragePaths, i, m) = X4a / t;
    MLET(VarianceInt, i, m) = X2a;
}

}
// End of the NbrMCsimulation iterations
return OK;
}

#endif //PremiaCurrentVersion

```